

# An estimate of equilibrium climate sensitivity from interannual variability

A. E. Dessler

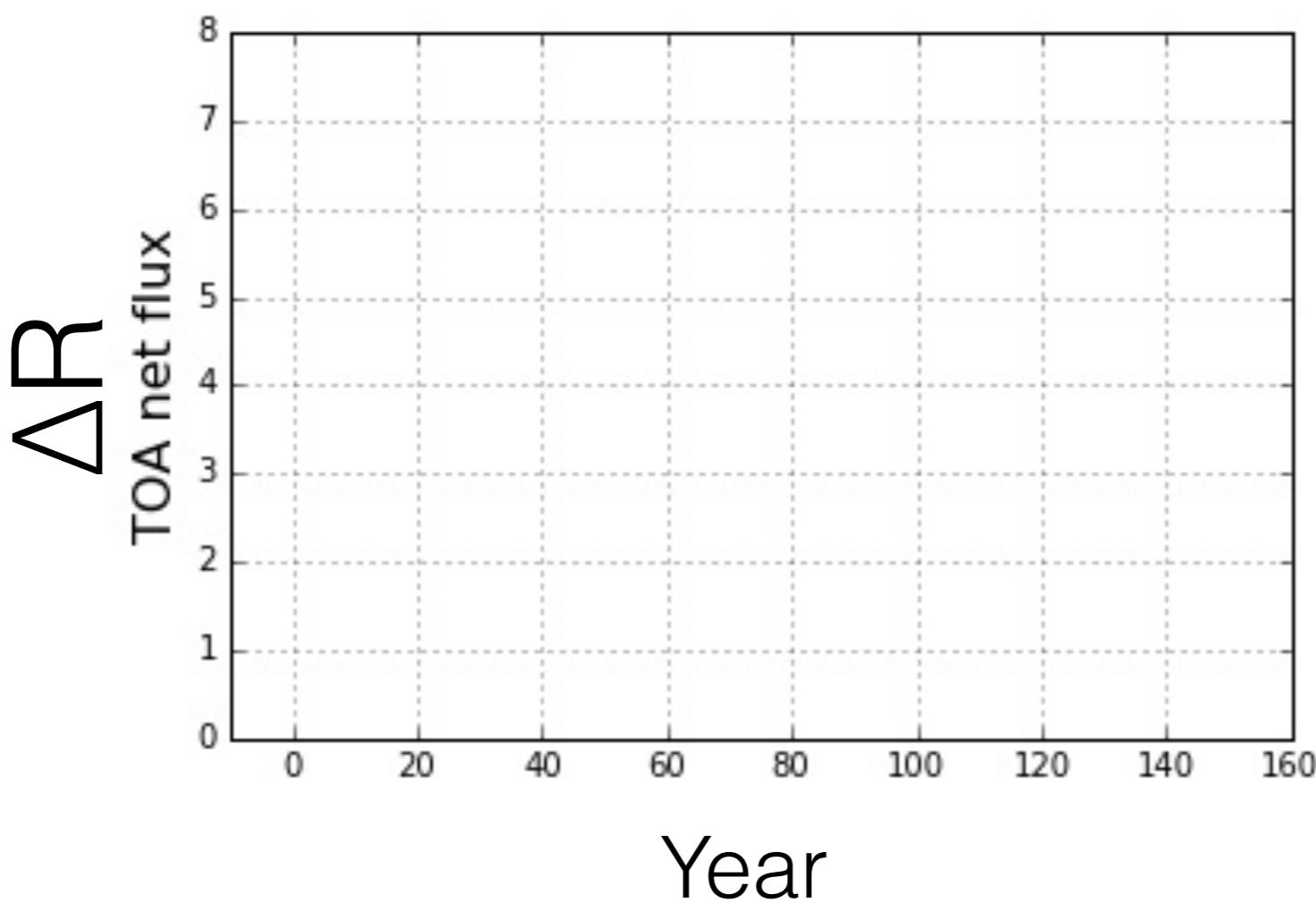
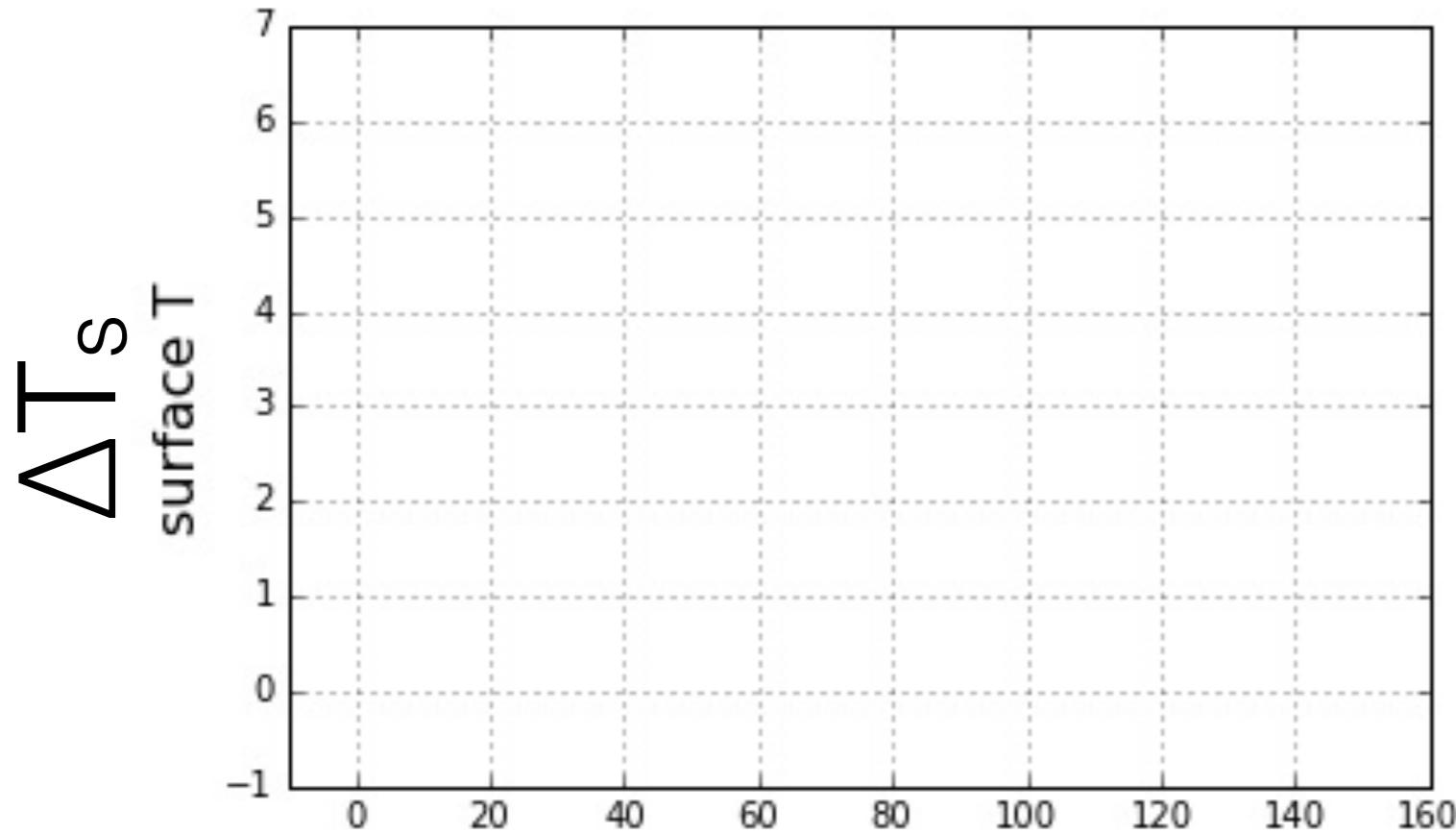
Dept. of Atmospheric Sciences  
Texas A&M University

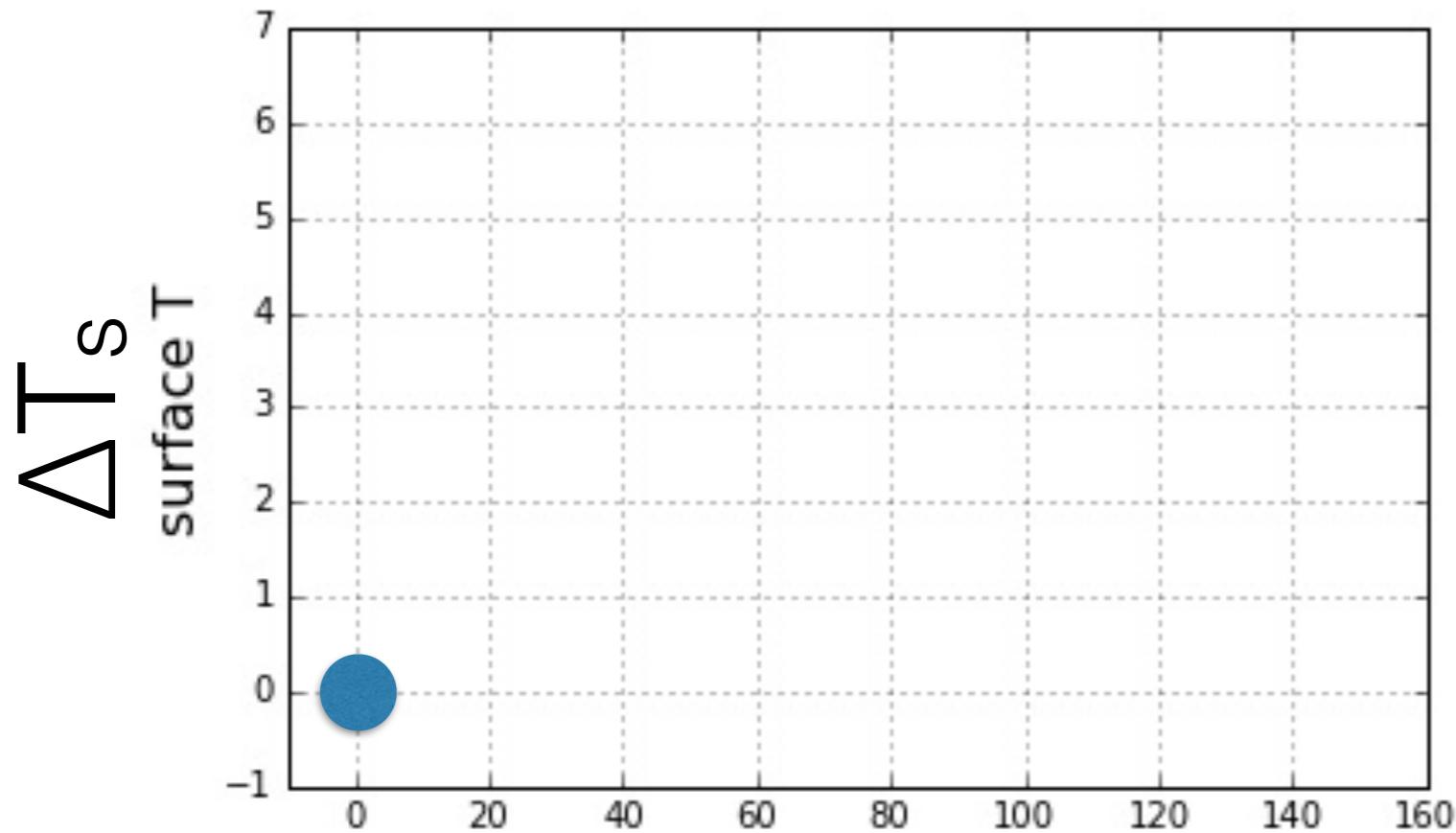
P. M. Forster

School of Earth and Environment  
University of Leeds

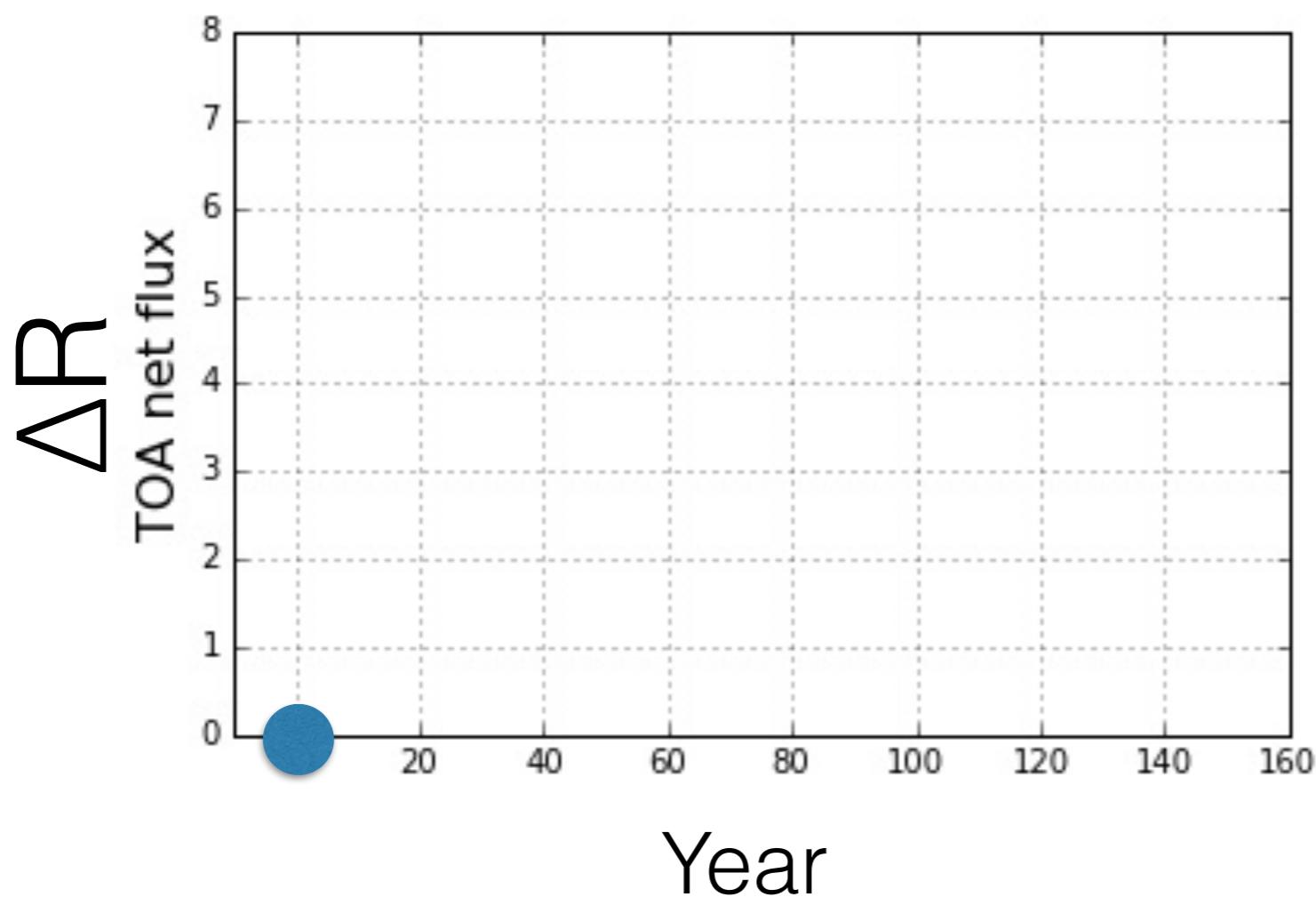


abrupt 4xCO<sub>2</sub>  
GFDL-CM3

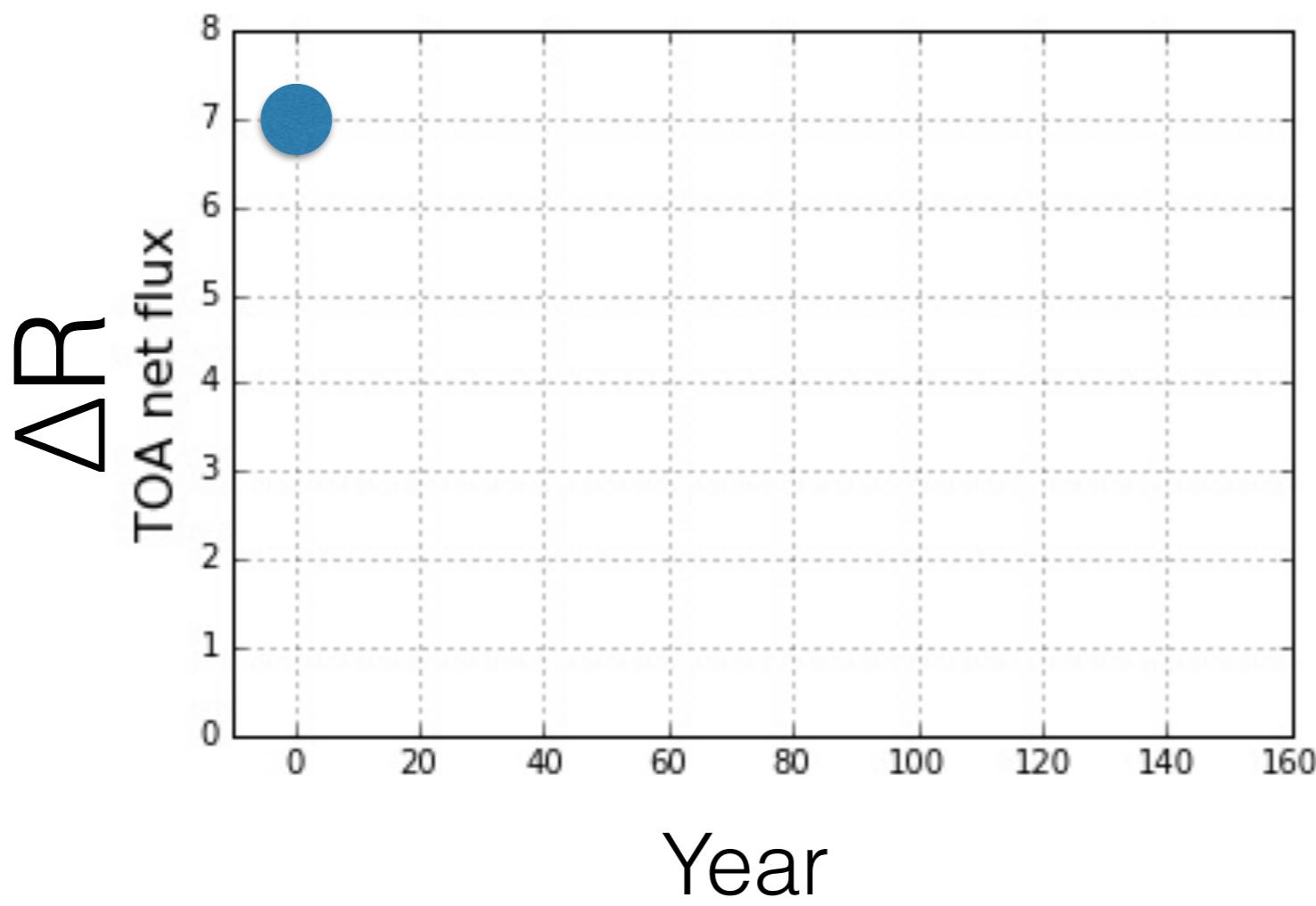
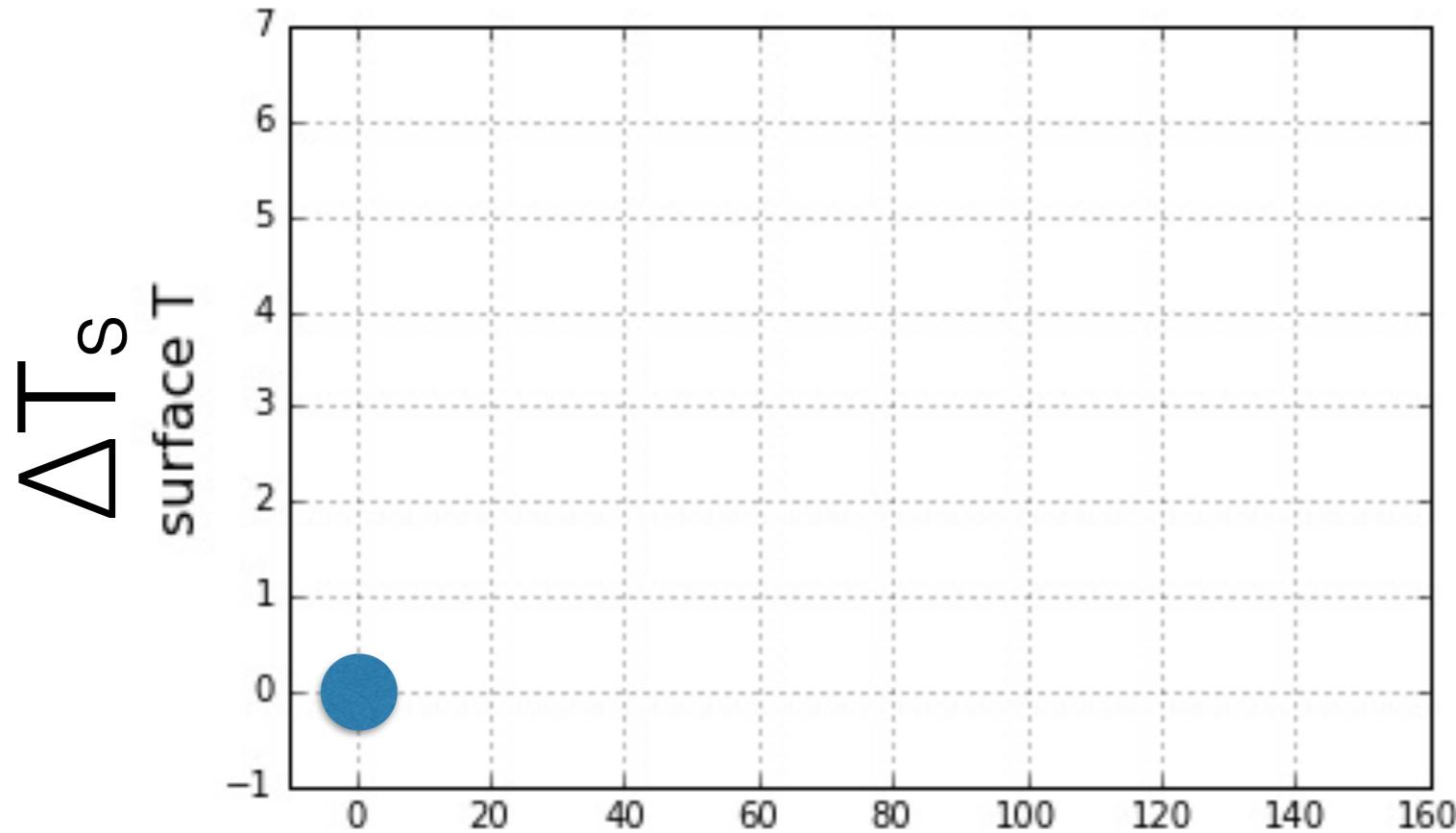




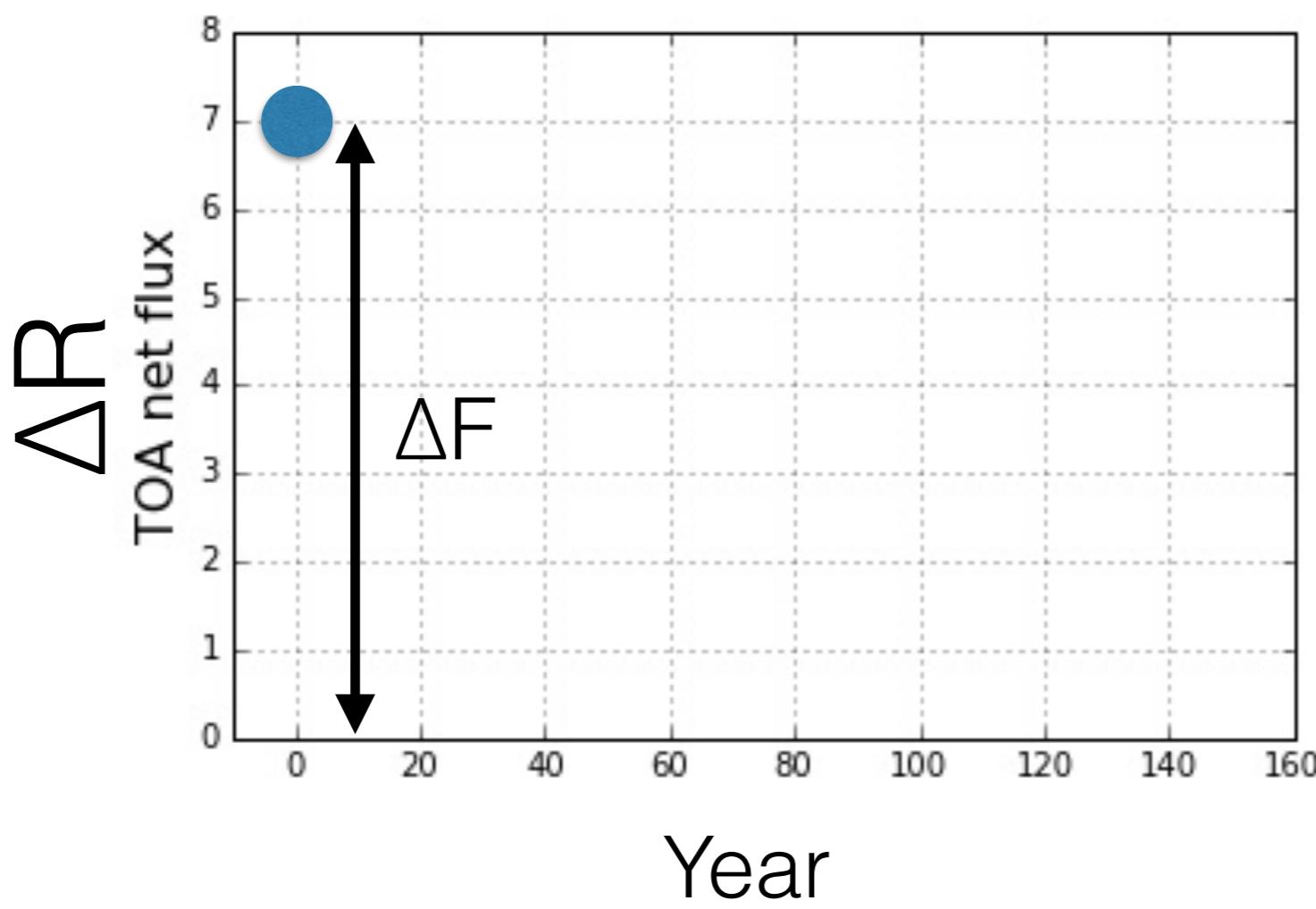
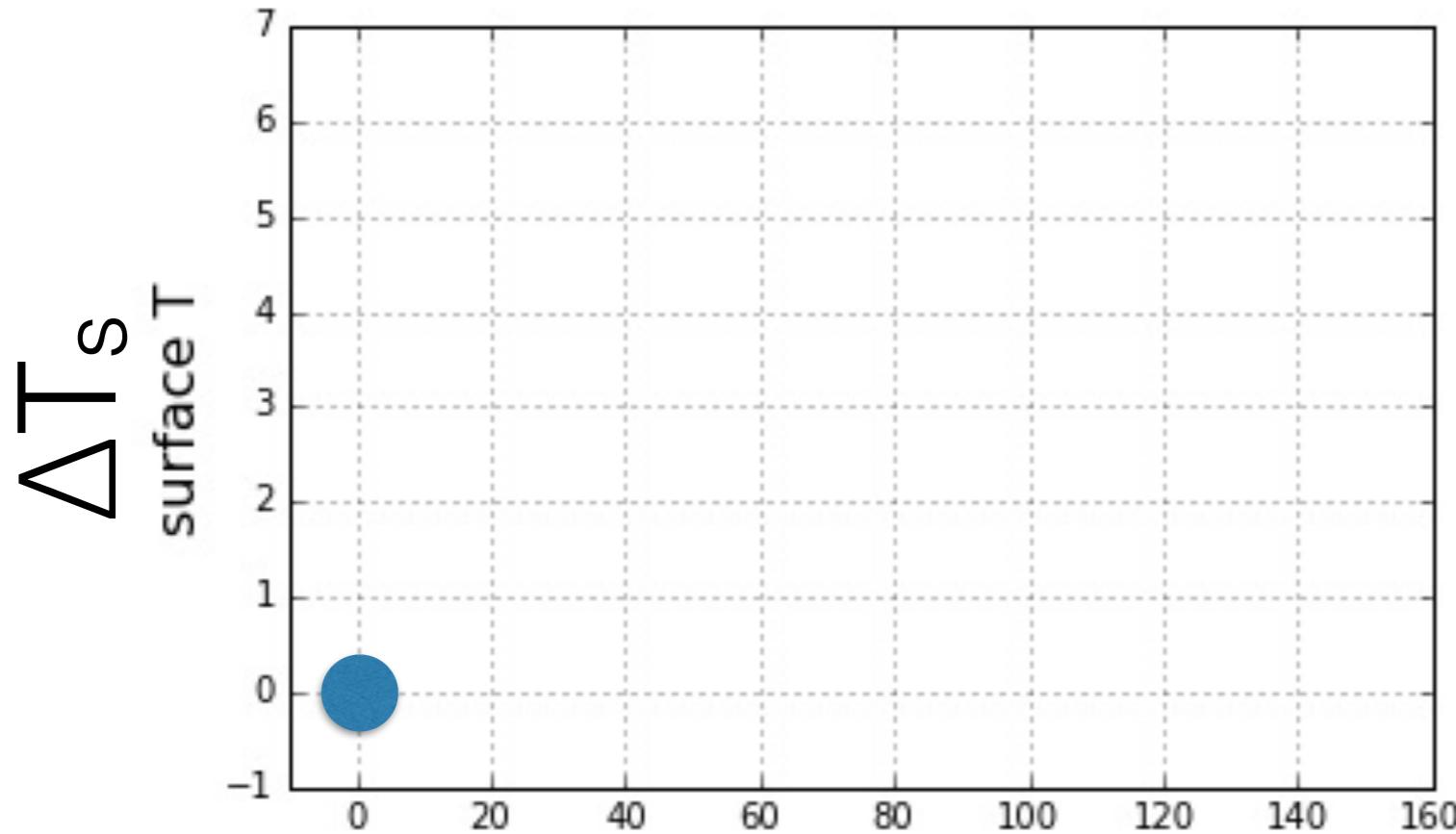
abrupt  $4\times CO_2$   
GFDL-CM3

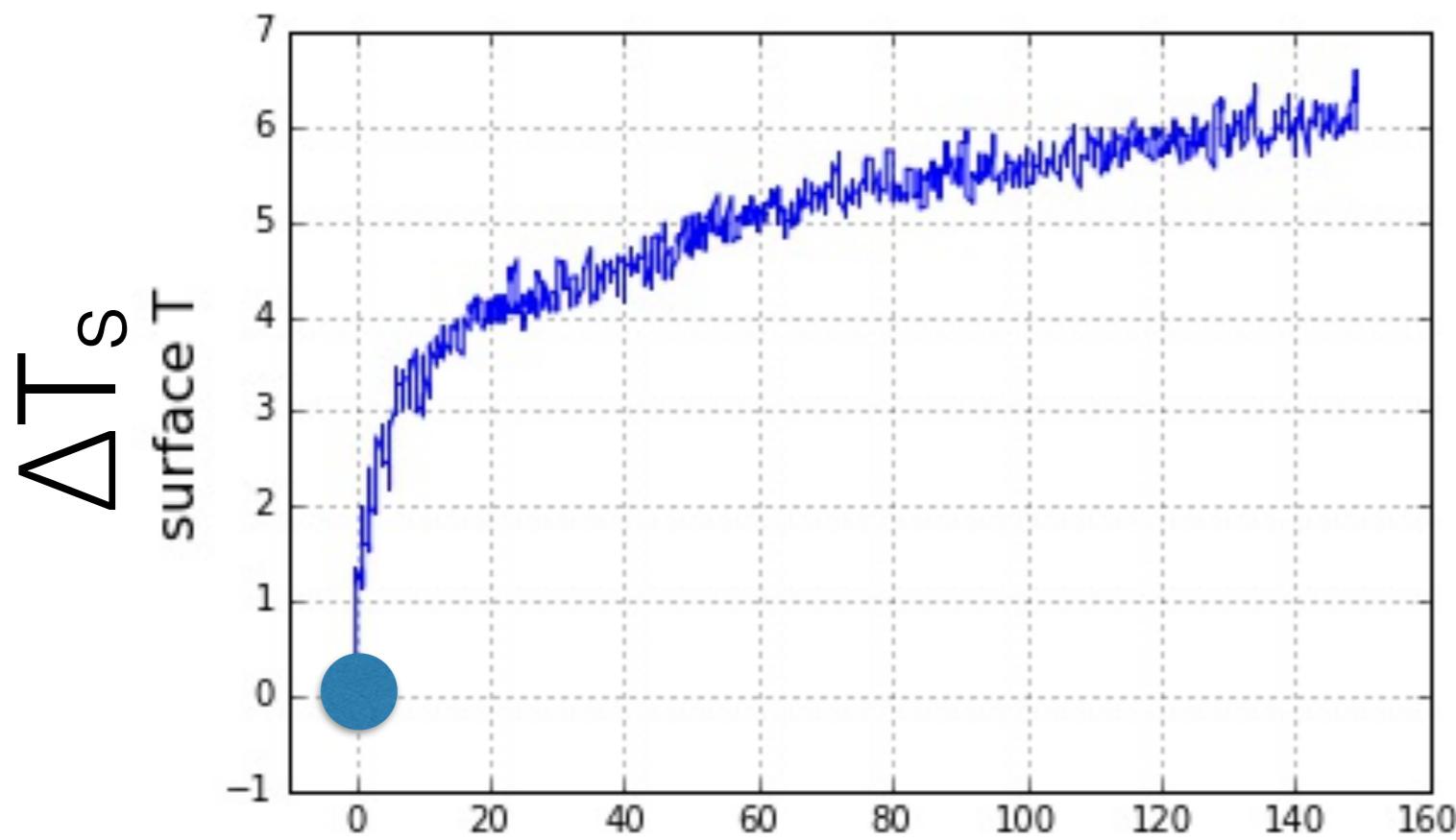


abrupt 4xCO<sub>2</sub>  
GFDL-CM3

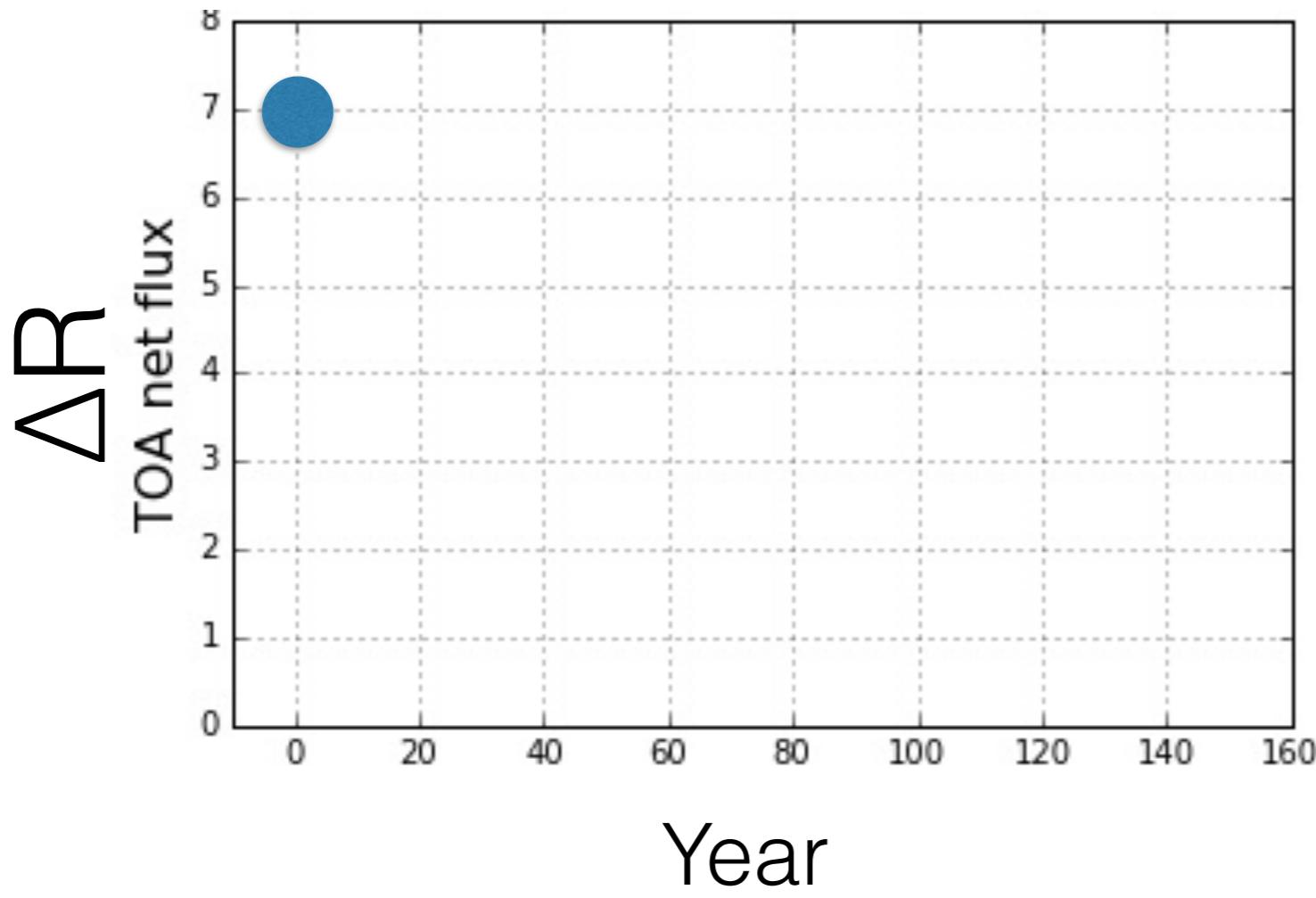


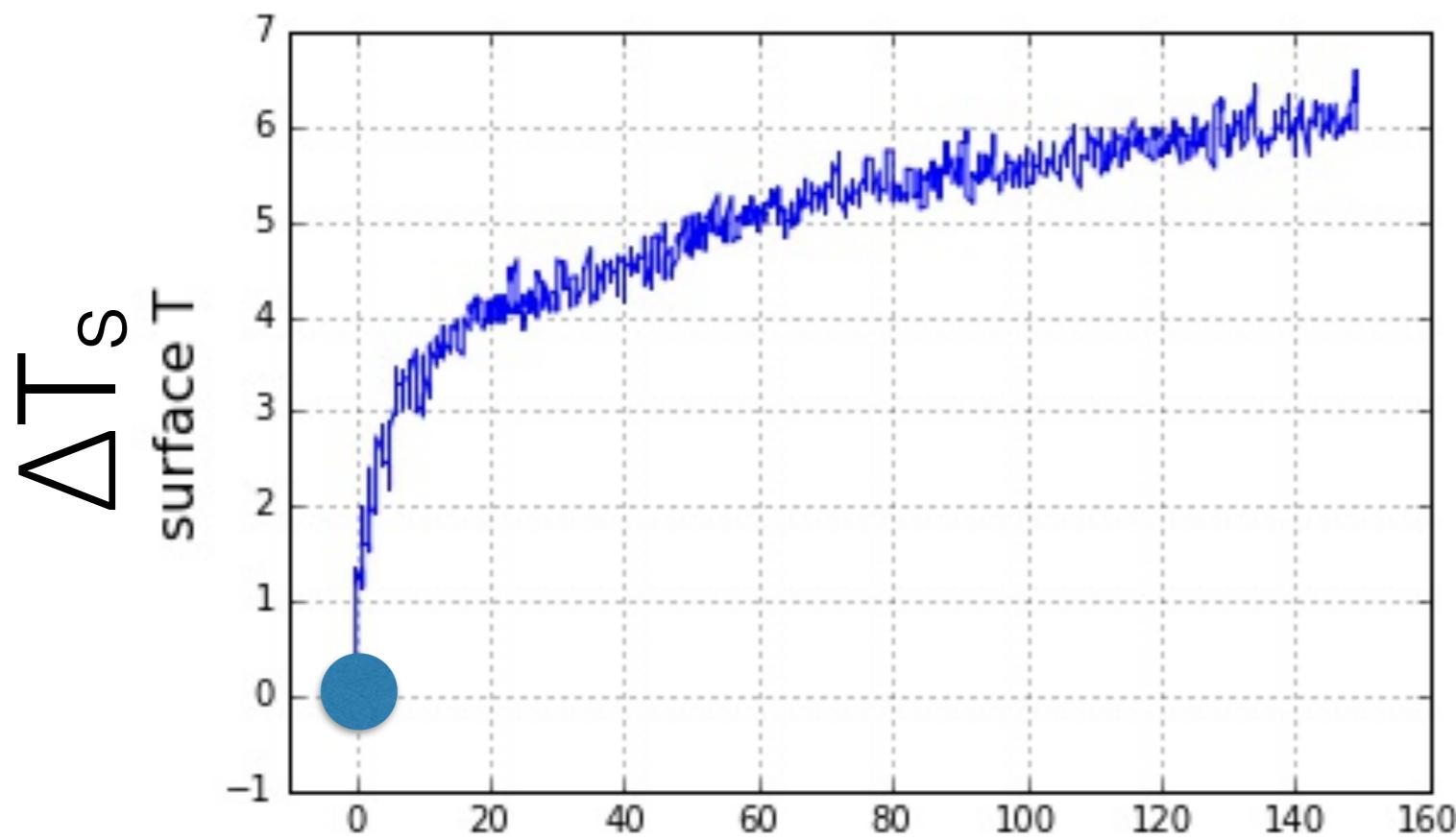
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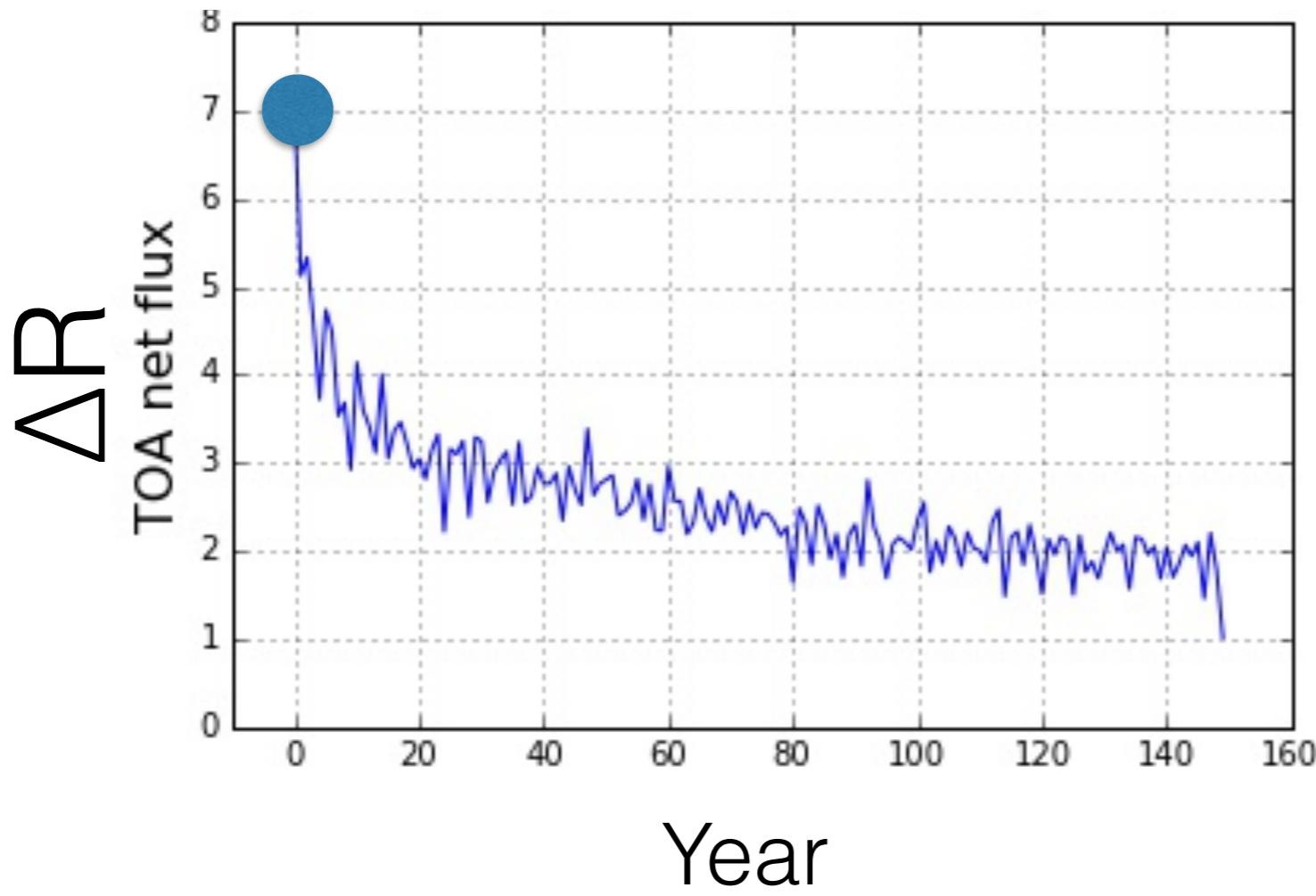


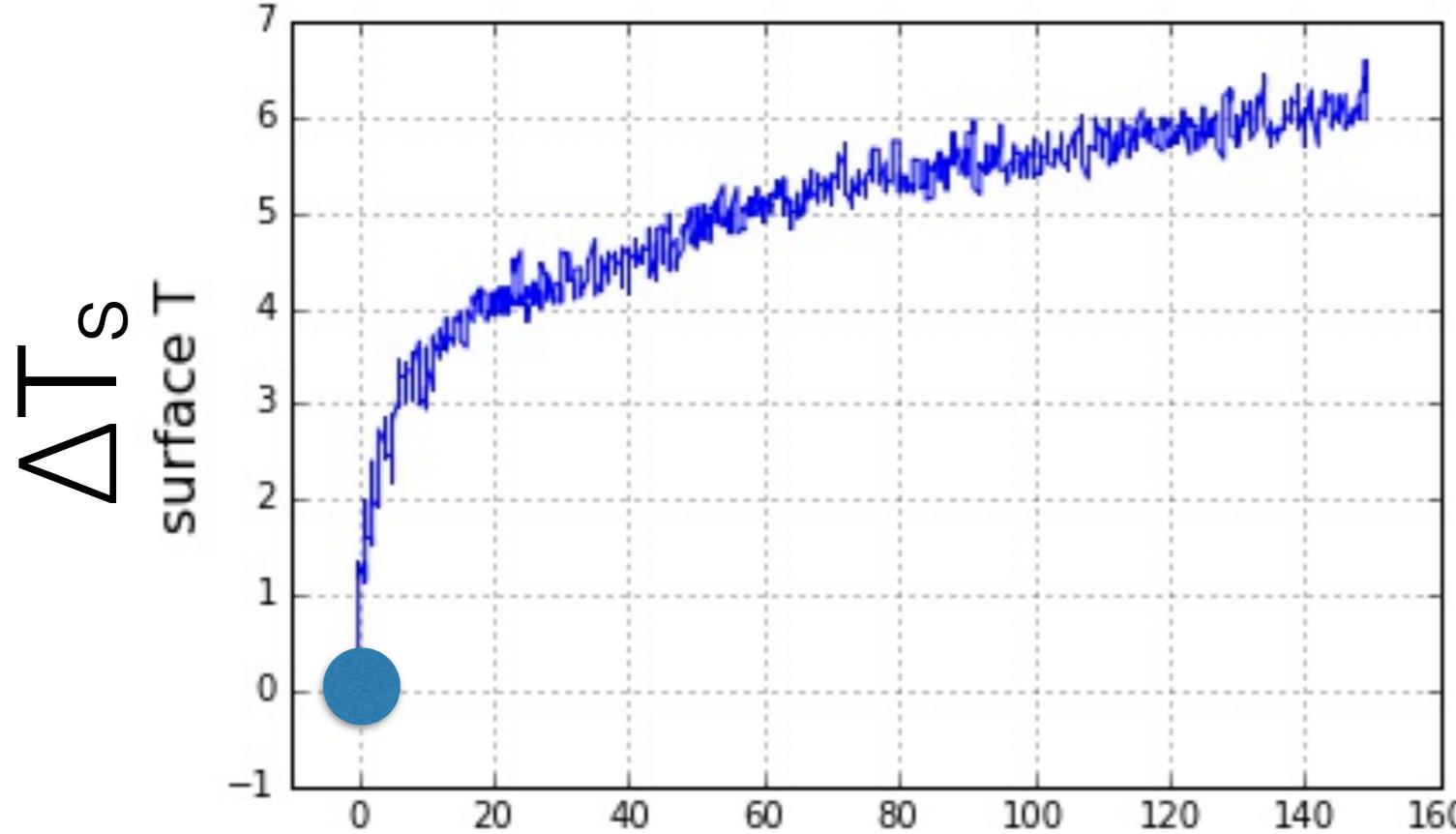
abrupt 4xCO2  
GFDL-CM3



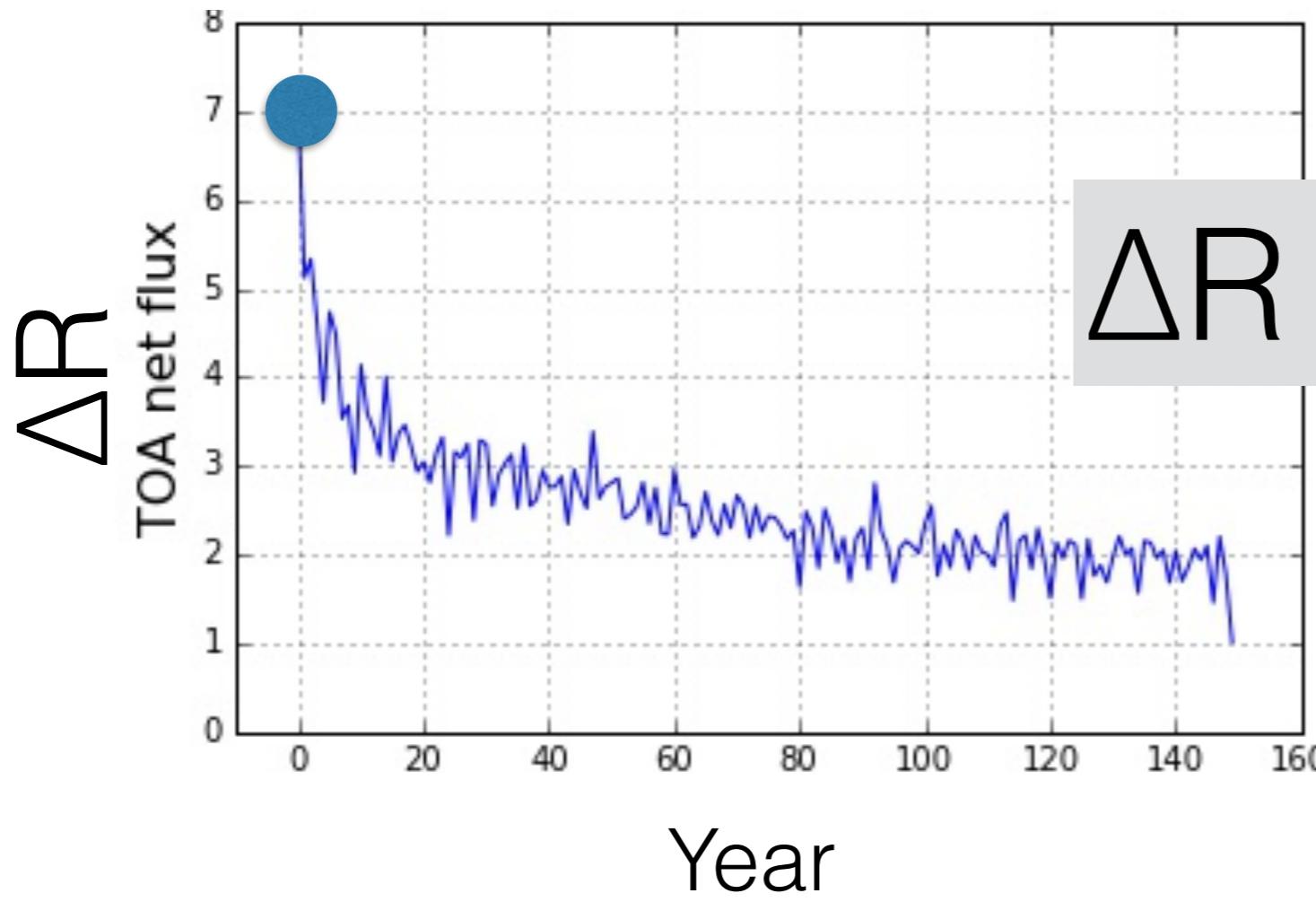


abrupt 4xCO<sub>2</sub>  
GFDL-CM3





abrupt 4xCO<sub>2</sub>  
GFDL-CM3



$$\Delta R = \Delta F + \lambda \Delta T_S$$

$$\Delta R = \Delta F + \lambda \Delta T_S$$



solve for this

$$\Delta R = \Delta F + \lambda \Delta T_S$$



$$ECS = -\frac{F_{2\times CO_2}}{\lambda}$$

$$\Delta R = \Delta F + \lambda \Delta T_S$$



solve for this

$$\Delta R = \Delta F + \lambda \Delta T_S$$

CERES

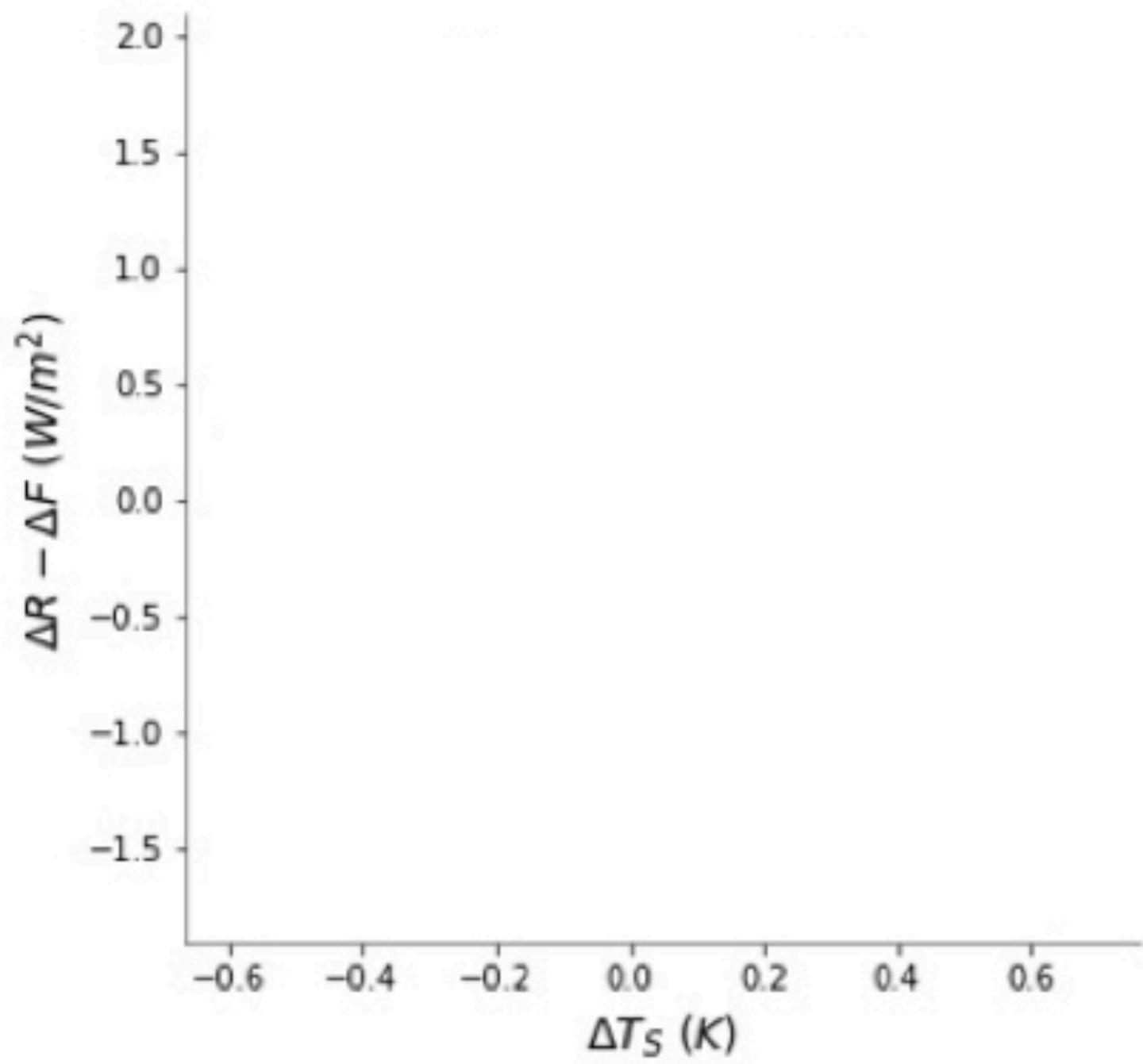
updated AR/5

solve for this

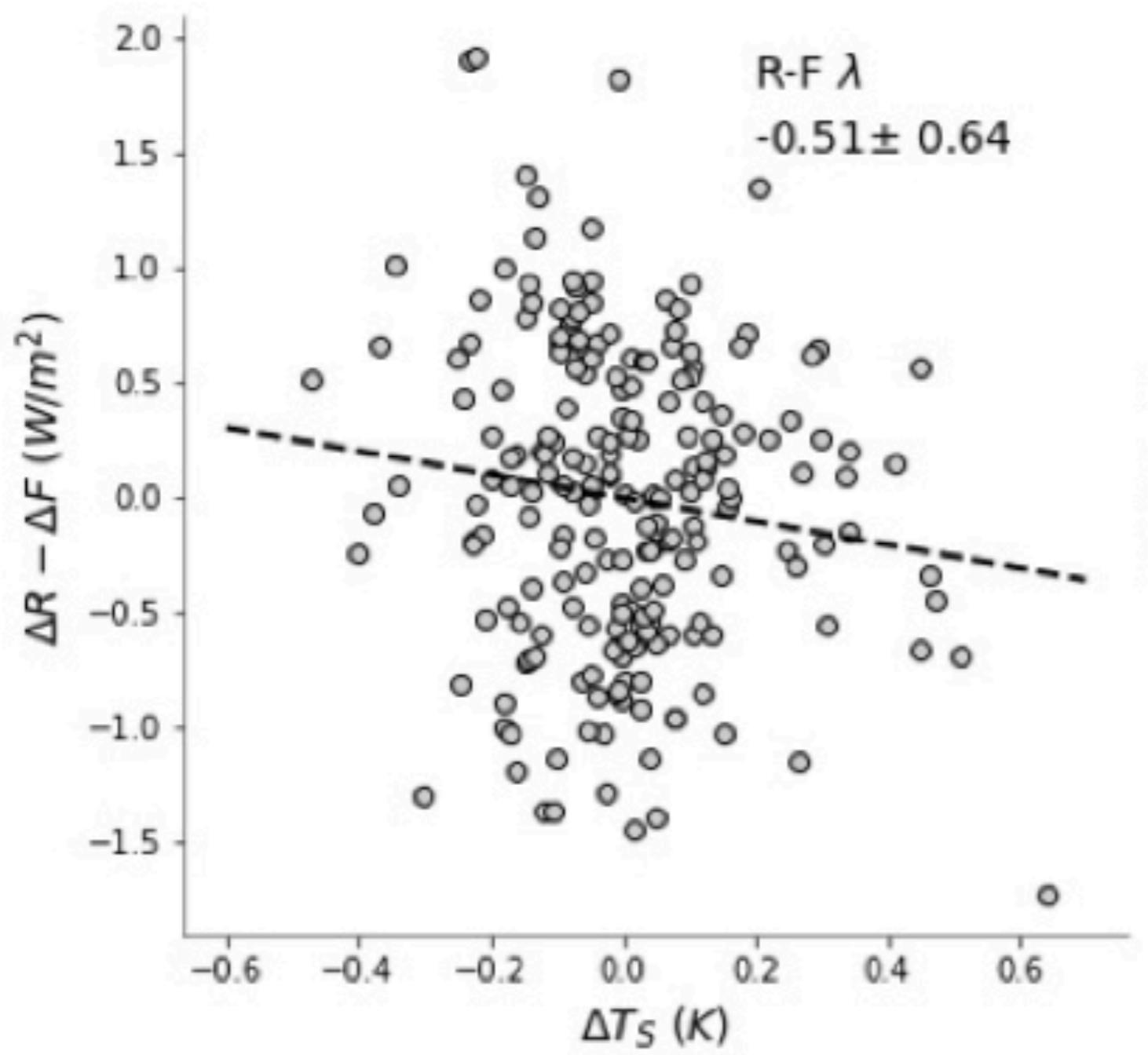
ERA-interim

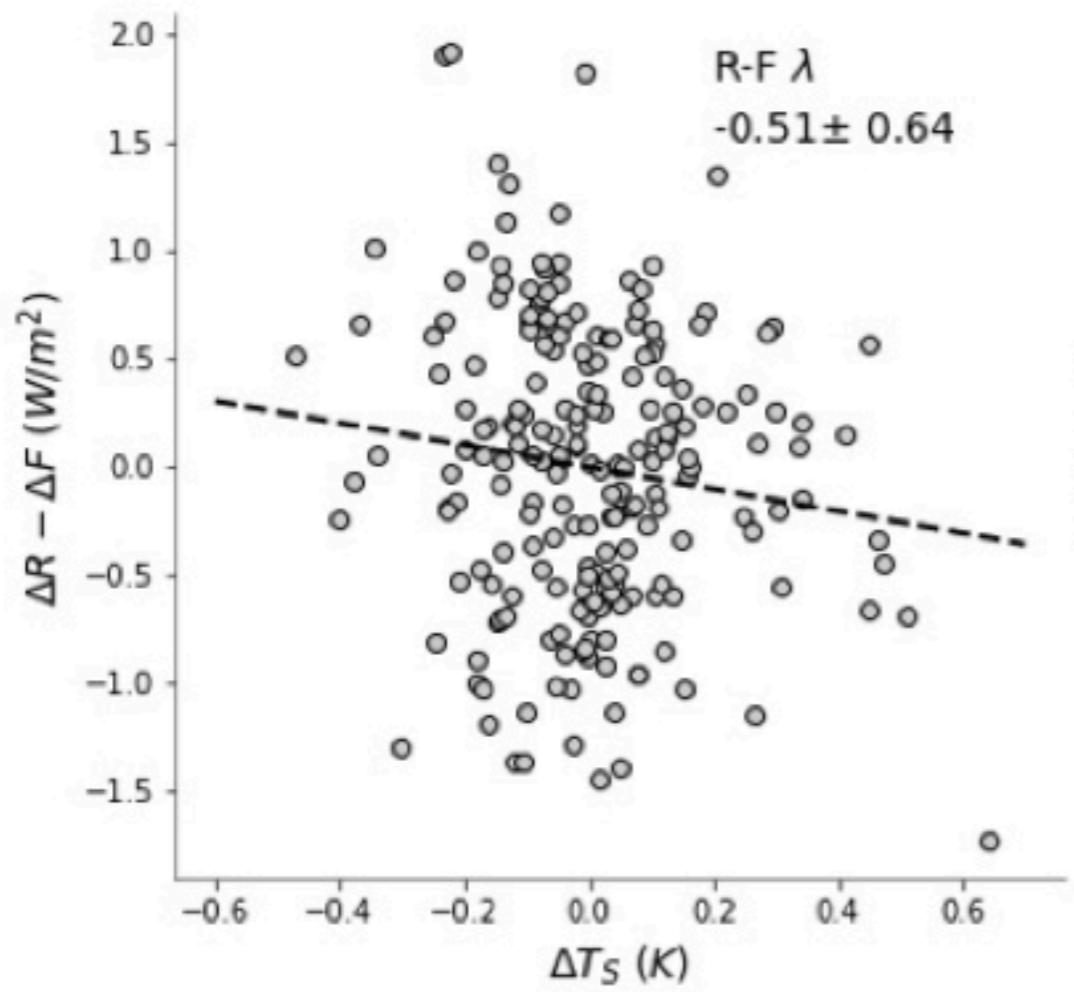
analysis covers 2000-2017

$$\Delta R - \Delta F = \lambda \Delta T_S$$

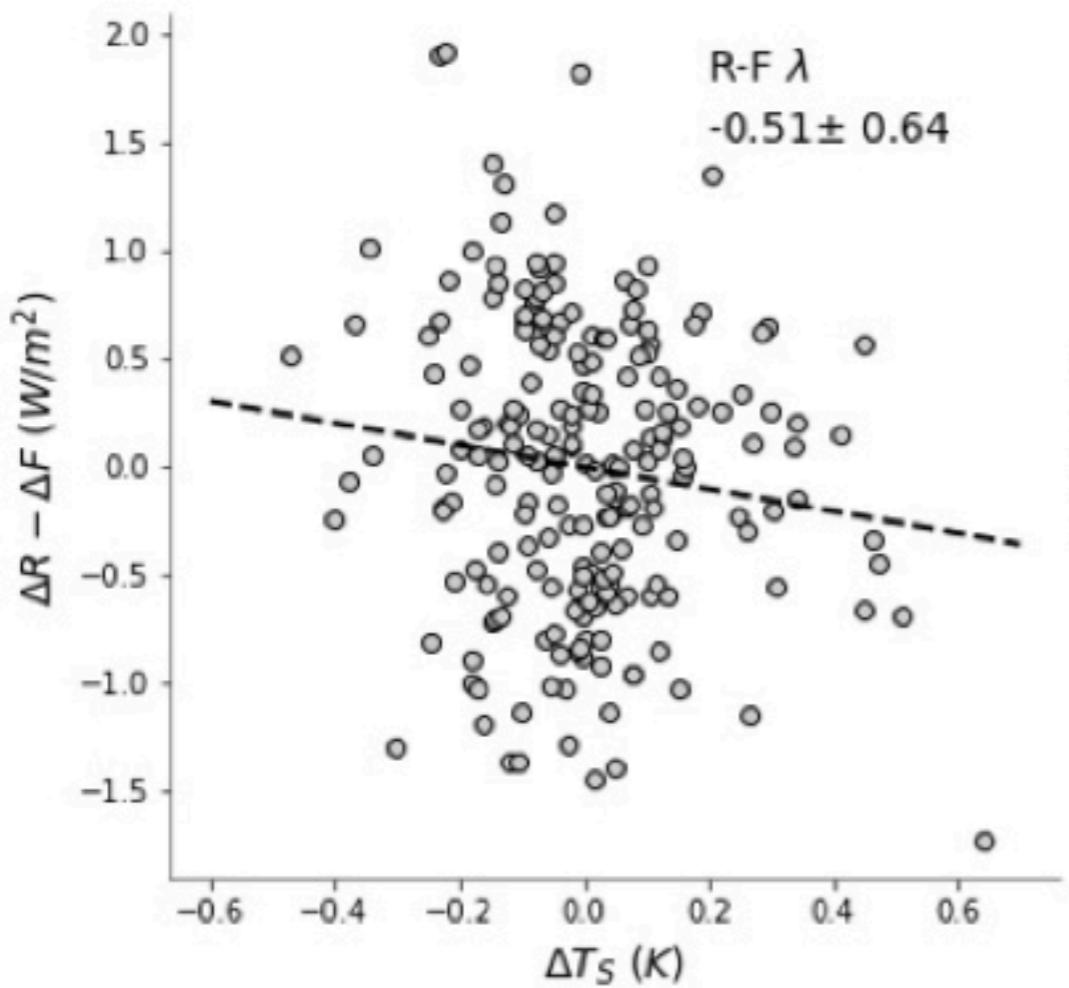


$$\Delta R - \Delta F = \lambda \Delta T_S$$



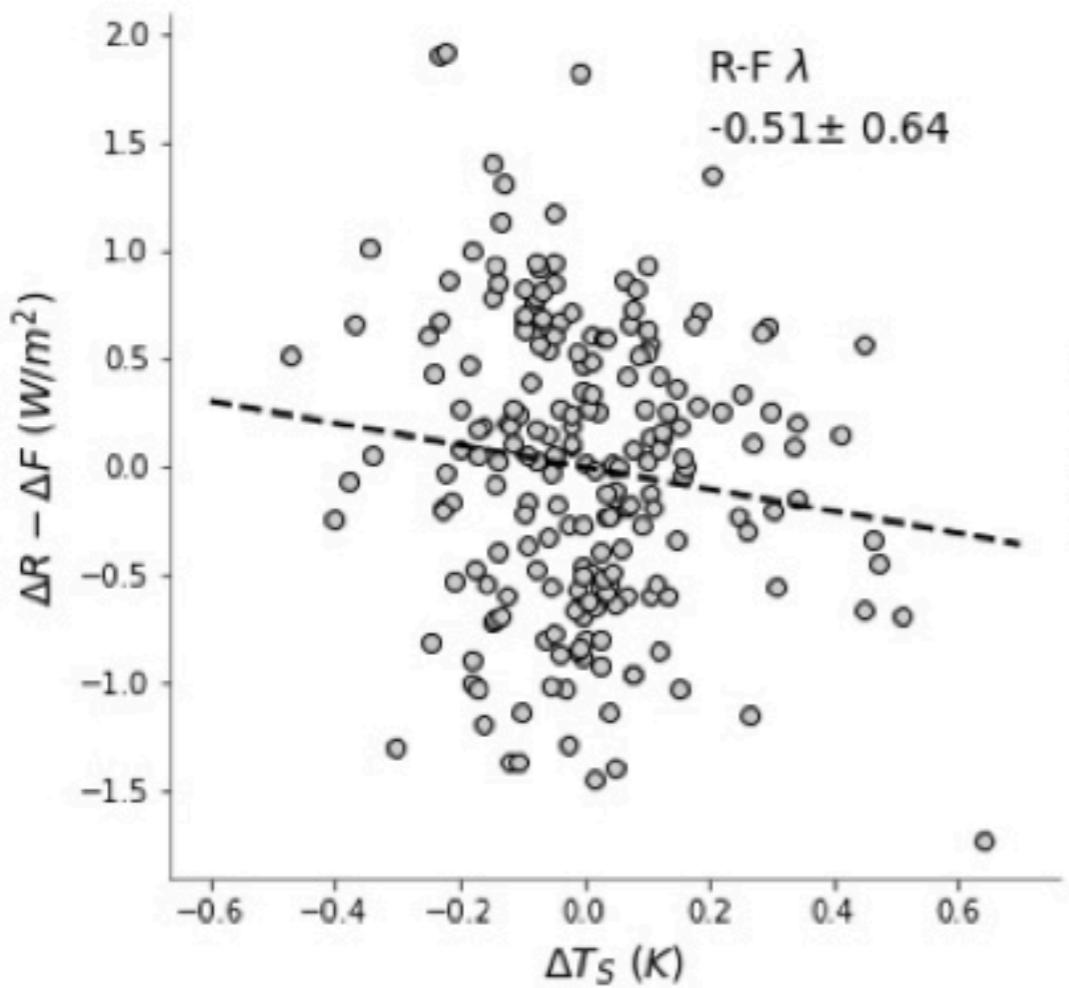


$\lambda_{iv}$



$$ECS = -\frac{F_2 \times CO_2}{\lambda_2 \times CO_2}$$

$\lambda_{iv}$



$$ECS = -\frac{F_2 \times CO_2}{\lambda_2 \times CO_2}$$

???

$\lambda_{iv}$

$$\lambda_{2\times CO_2,est} = \lambda_{iv,obs}\left(\frac{\lambda_{2\times CO_2}}{\lambda_{iv}}\right)$$

$$\lambda_{2\times CO_2,est} = \lambda_{iv,obs} \left( \frac{\lambda_{2\times CO_2}}{\lambda_{iv}} \right)$$

Measured by CERES

$$\lambda_{2\times CO_2,est} = \lambda_{iv,obs} \left( \frac{\lambda_{2\times CO_2}}{\lambda_{iv}} \right)$$

Measured by CERES

estimated from  
CMIP5 model runs

# Traditional energy balance framework

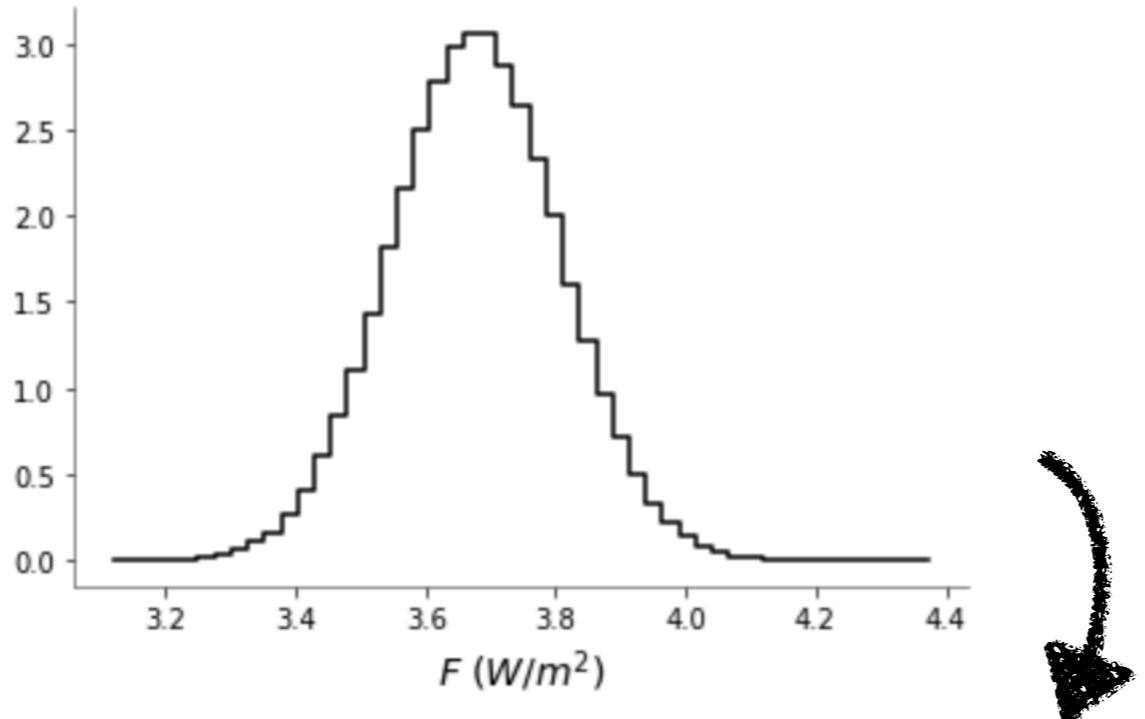
$$\text{ECS} = -\frac{F_{2\times CO_2}}{\lambda_{iv,obs}} \left( \frac{\lambda_{iv}}{\lambda_{2\times CO_2}} \right)$$

# Traditional energy balance framework

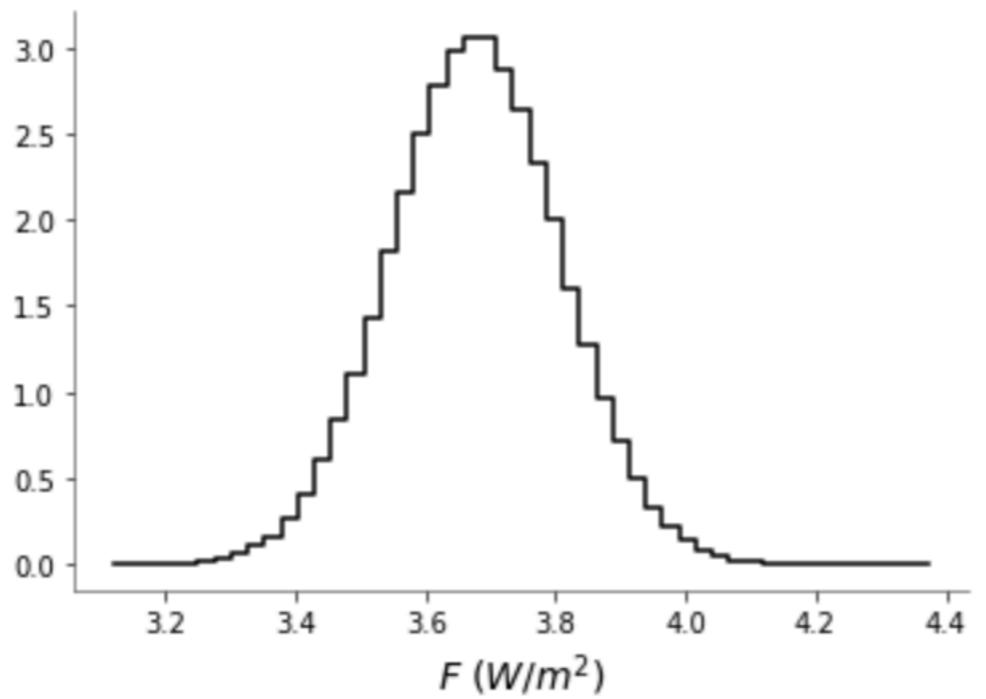
$$\text{ECS} = -\frac{F_{2\times CO_2}}{\lambda_{iv,obs}} \left( \frac{\lambda_{iv}}{\lambda_{2\times CO_2}} \right)$$

$$\text{ECS} \approx -\frac{F_{2\times CO_2}}{\lambda_{iv,obs}} \left( \frac{\lambda_{iv}}{\lambda_{4\times CO_2}} \right)$$

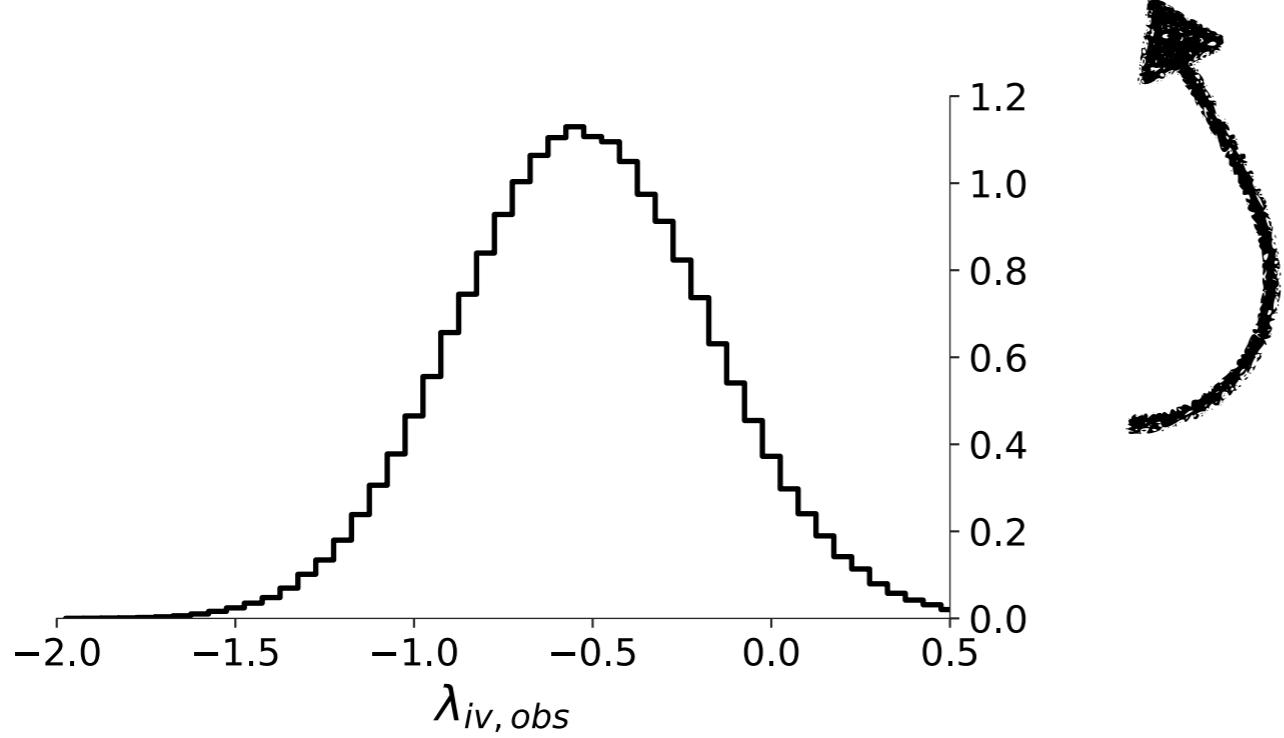
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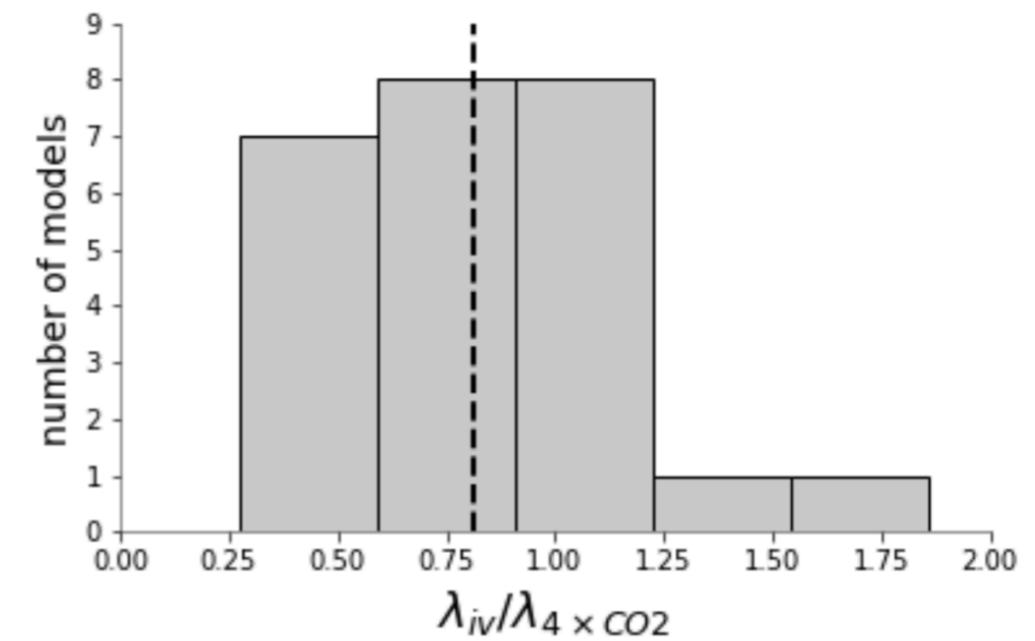
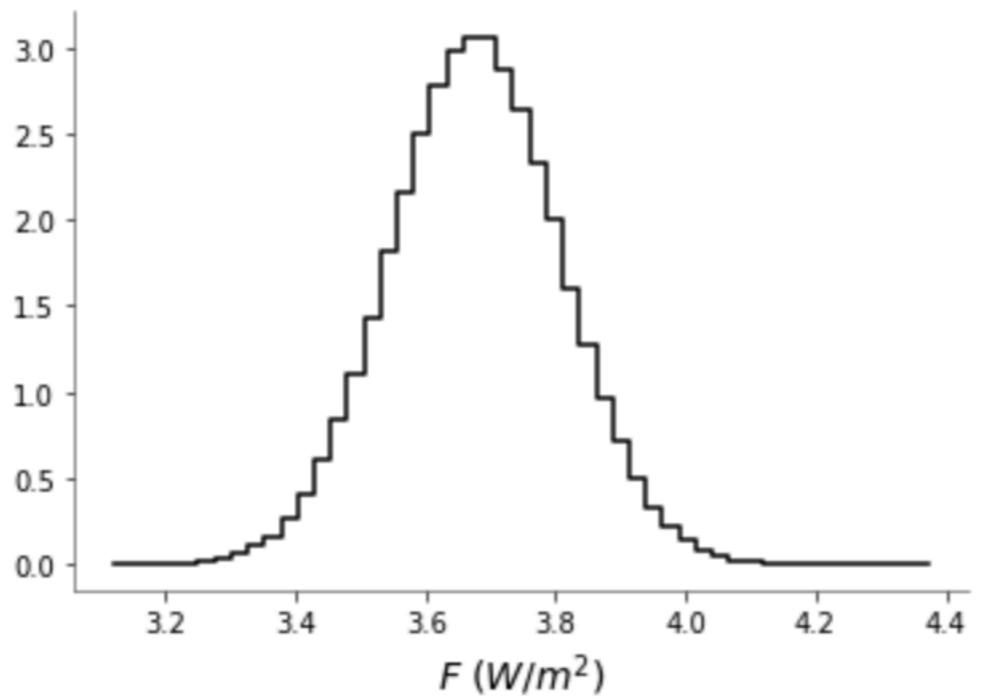


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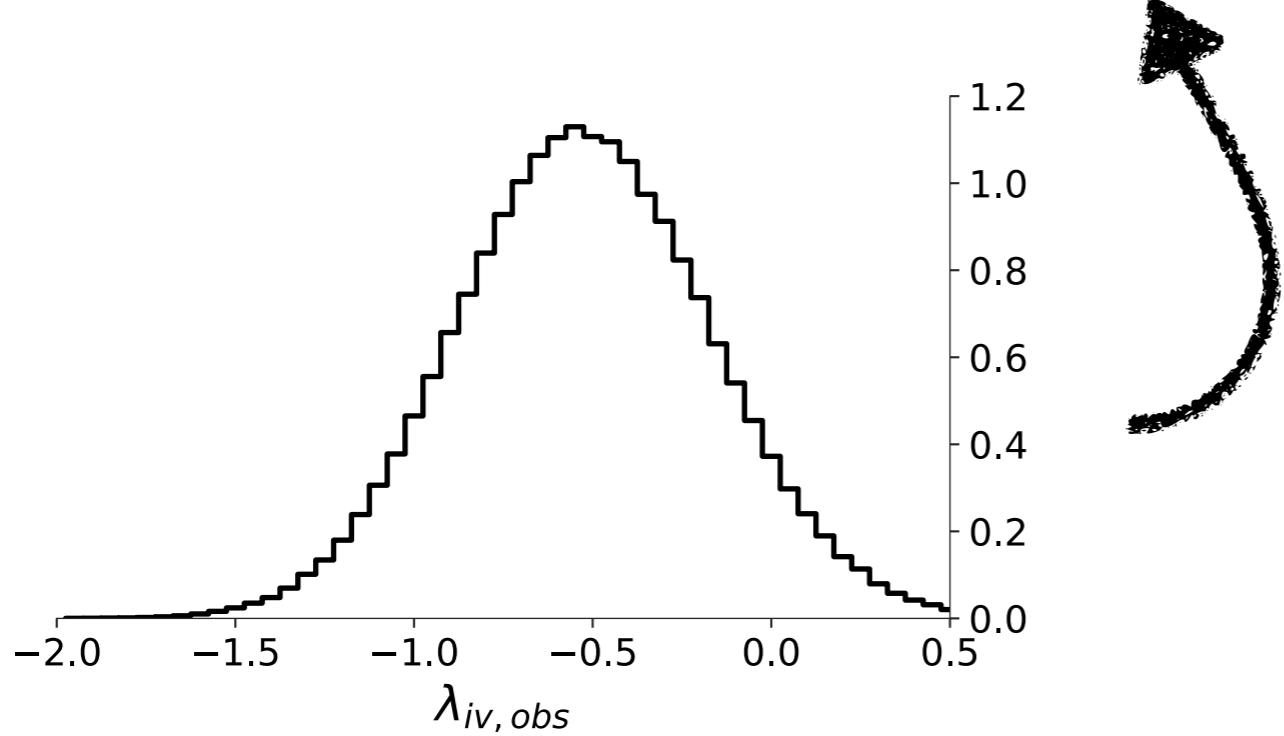


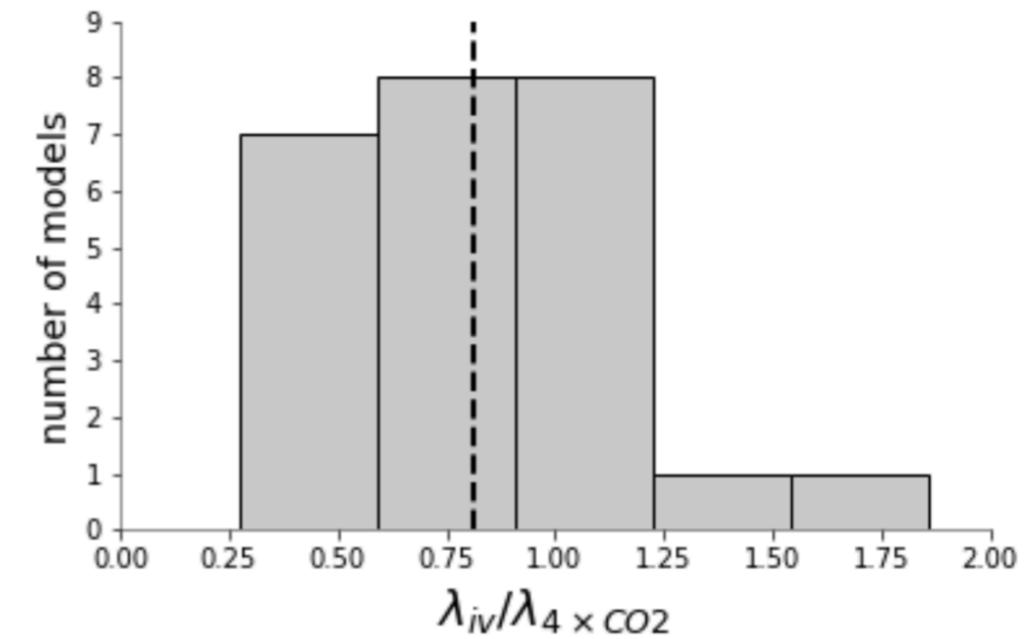
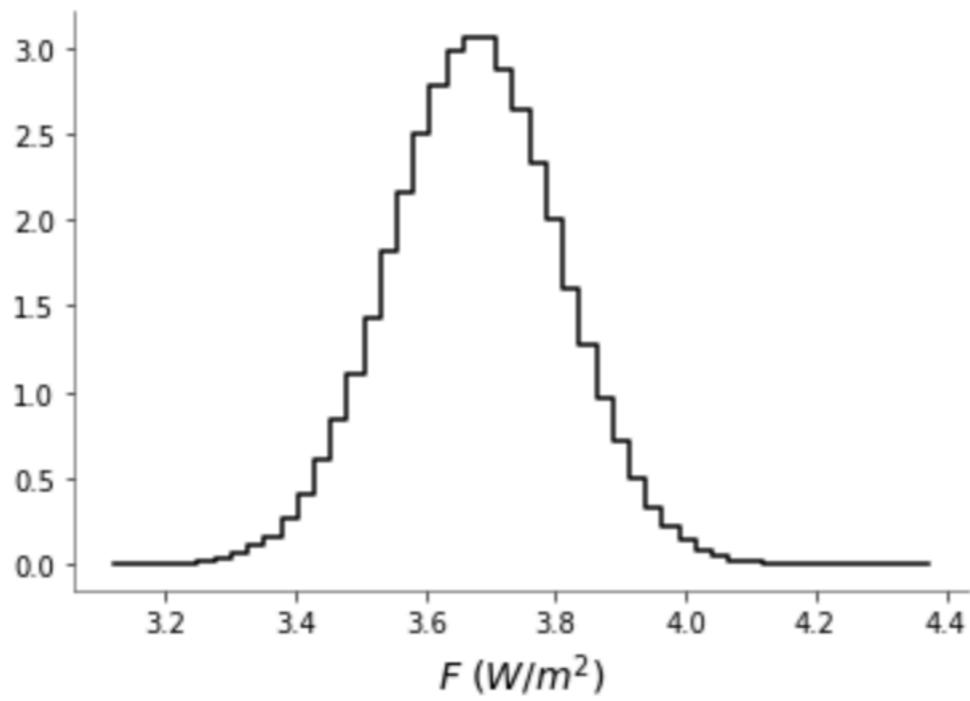
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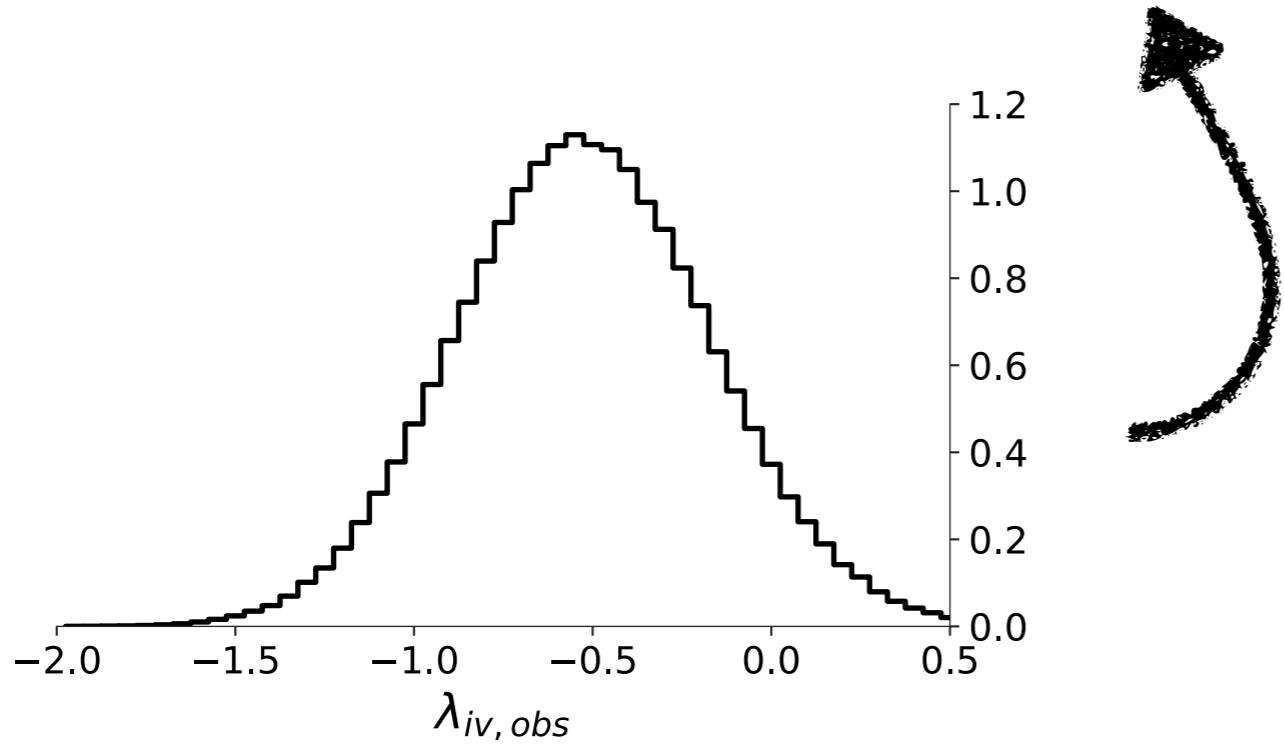


$$\text{ECS} \approx -\frac{F_{2 \times \text{CO}_2}}{\lambda_{iv,obs}} \left( \frac{\lambda_{iv}}{\lambda_{4 \times \text{CO}_2}} \right)$$



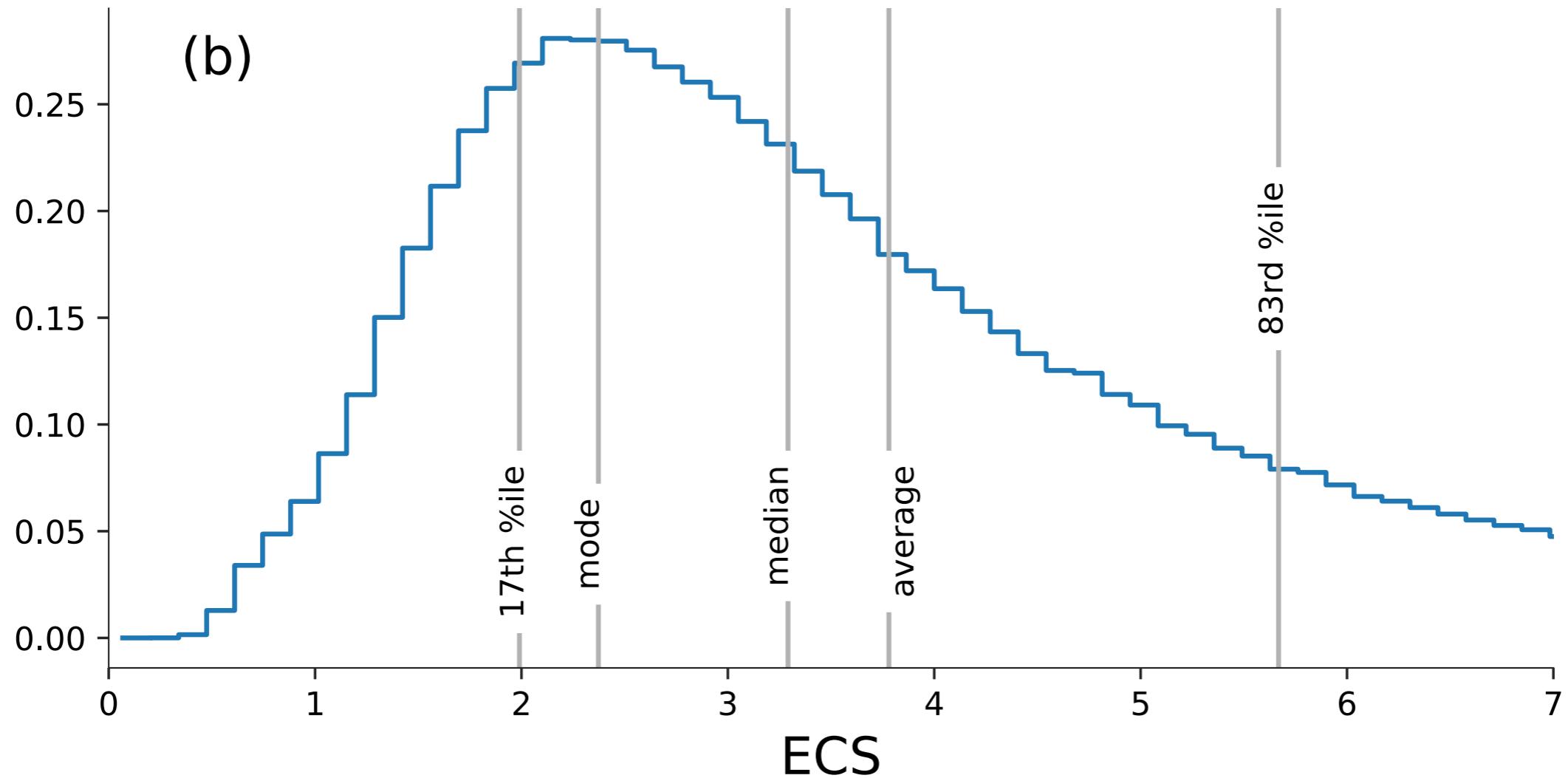


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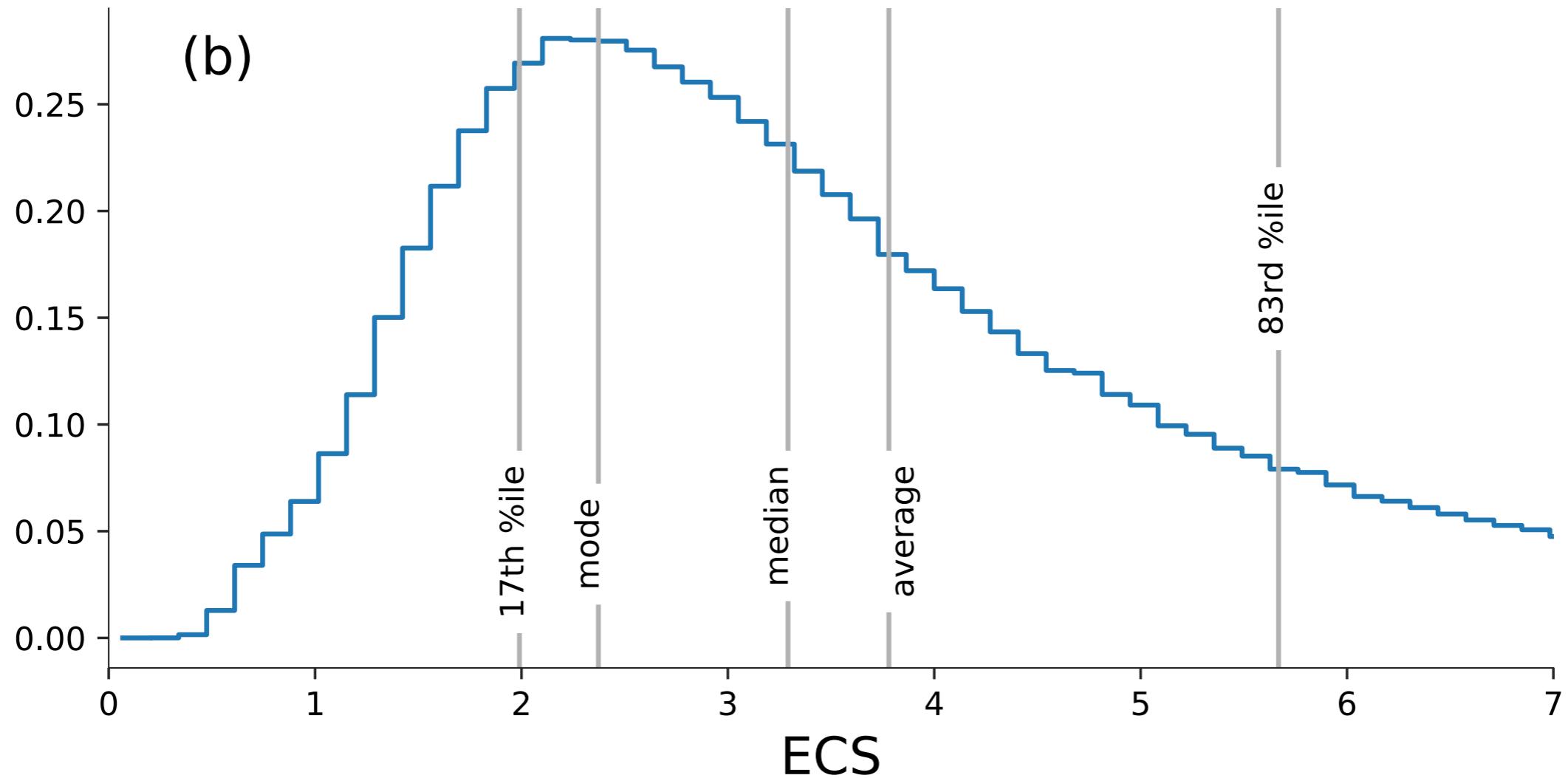


Monte Carlo: take  
500,000 samples of  
each distribution and  
calculate 500,000  
estimates of ECS

# ECS



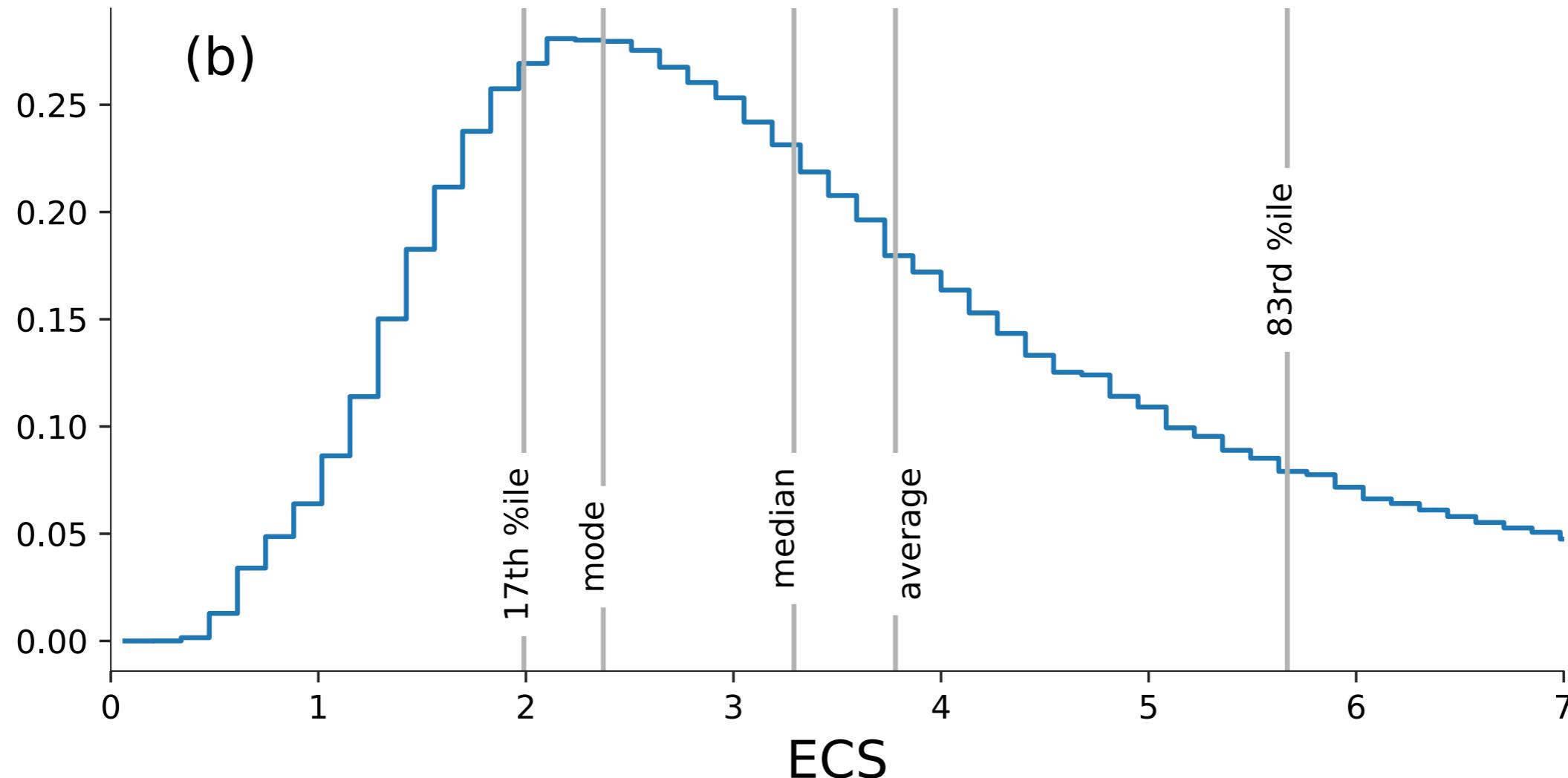
# ECS



*likely range:* 2.0-5.7 K  
median: 3.3 K



Problems: 1) not great constraint; 2)  $\lambda_{\text{iv,obs}}$  can vary



*likely* range: 2.0-5.7 K  
median: 3.3 K



# revised framework

$$R = F + \Theta \Delta T_A$$

Dessler, Mauritsen, Stevens: The influence of internal variability on Earth's energy balance framework and implications for estimating climate sensitivity, *Atmos. Chem. Phys.*, 2018.

# revised framework

$$R = F + \Theta \Delta T_A$$

500-hPa tropical  
temperatures



Dessler, Mauritsen, Stevens: The influence of internal variability on Earth's energy balance framework and implications for estimating climate sensitivity, *Atmos. Chem. Phys.*, 2018.

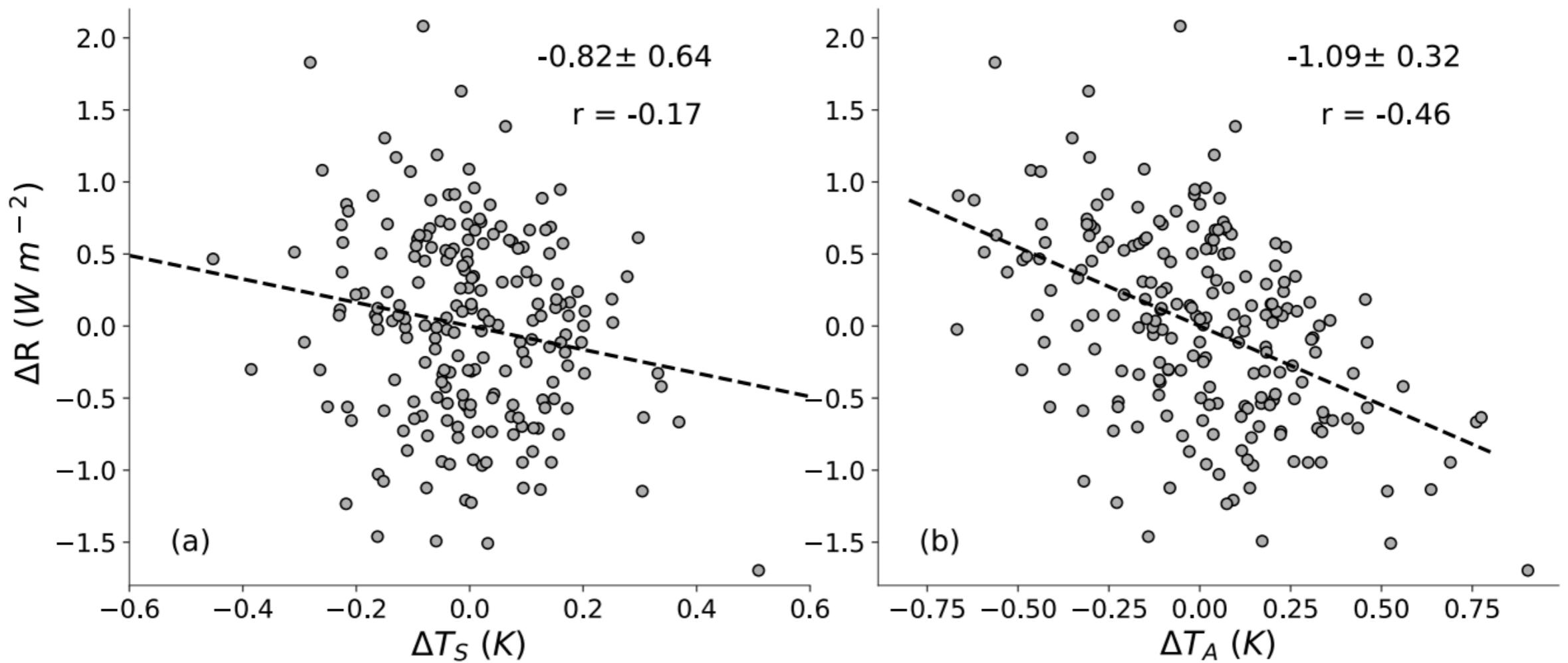
# revised framework

$$R = F + \Theta \Delta T_A$$

Converts change  
in  $T_A$  to flux;  
replaces  $\lambda$

500-hPa tropical  
temperatures

Dessler, Mauritsen, Stevens: The influence of internal variability  
on Earth's energy balance framework and implications for  
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CERES Ed. 4 TOA fluxes & ERA-interim  
temperatures

monthly avg. detrended anomalies

$\Delta T_s$  = global avg. surface temperature

$\Delta T_A$  = tropical avg. 500-hPa temperature

# revised framework

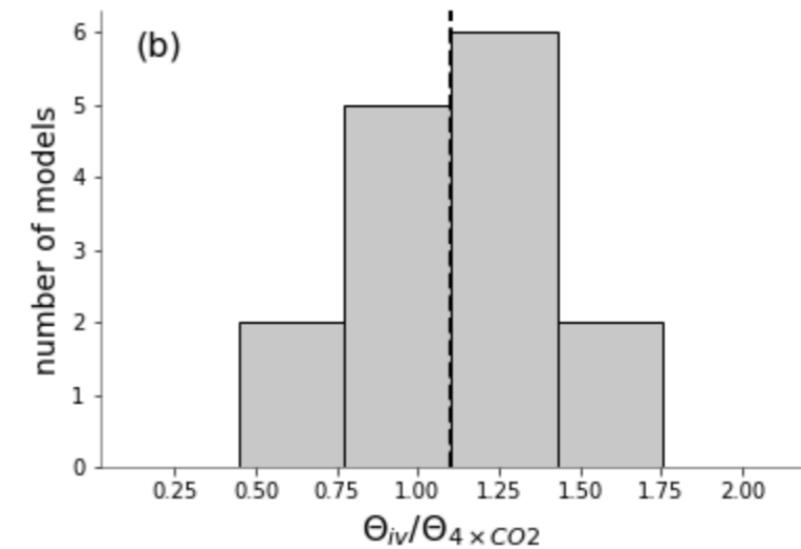
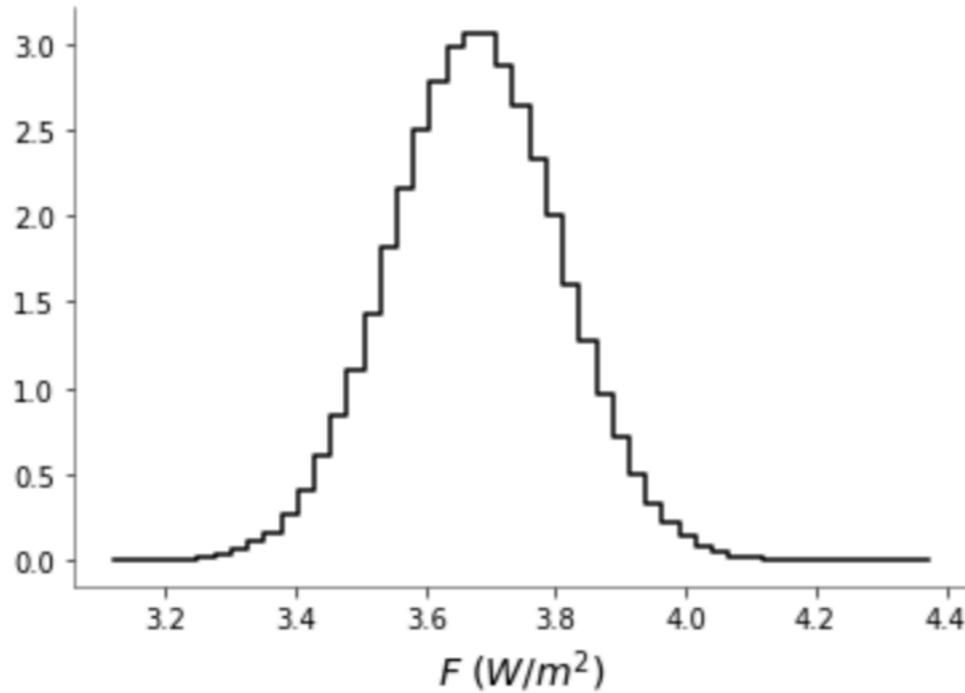
$$R = F + \Theta \Delta T_A$$

$$\text{ECS} \approx -\frac{F_{2\times CO_2}}{\Theta_{iv,obs}} \left( \frac{\Theta_{iv}}{\Theta_{4\times CO_2}} \right) \left( \frac{\Delta T_S}{\Delta T_A} \right)$$

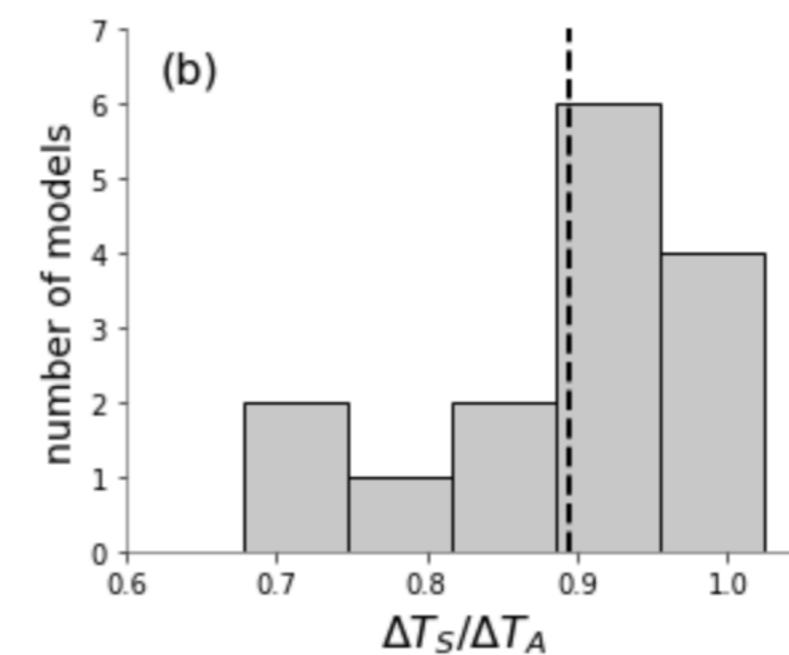
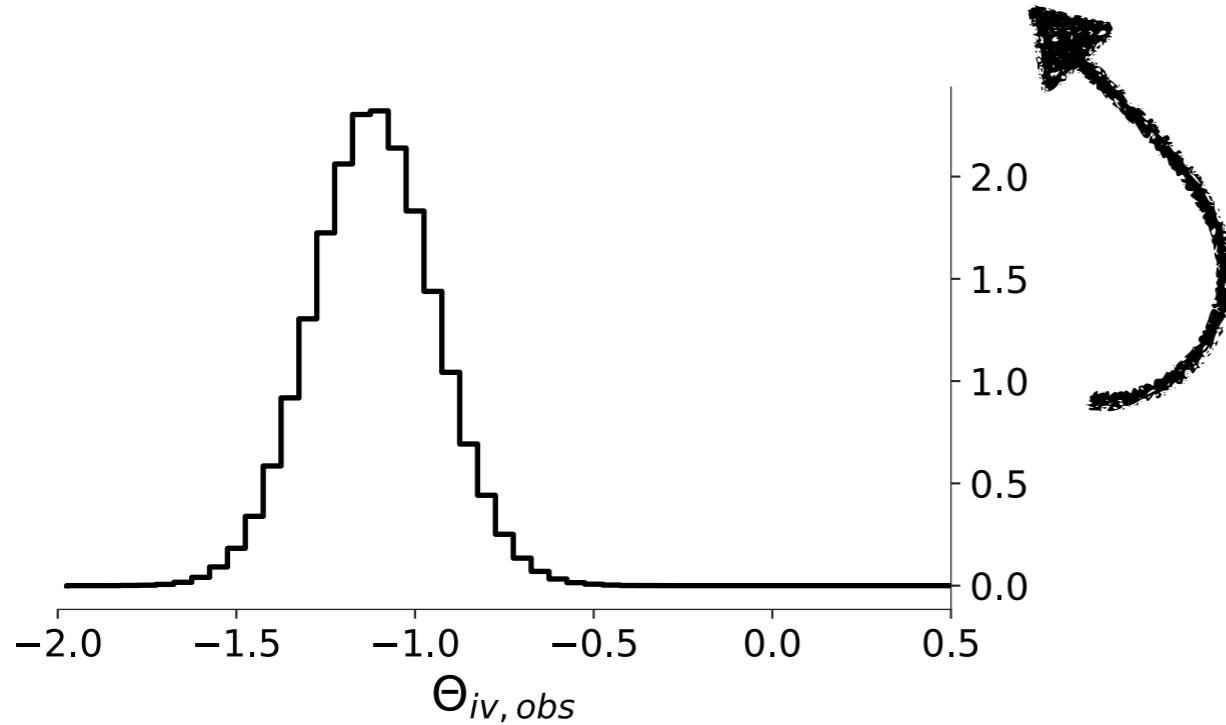
# revised framework

$$R = F + \Theta \Delta T_A$$

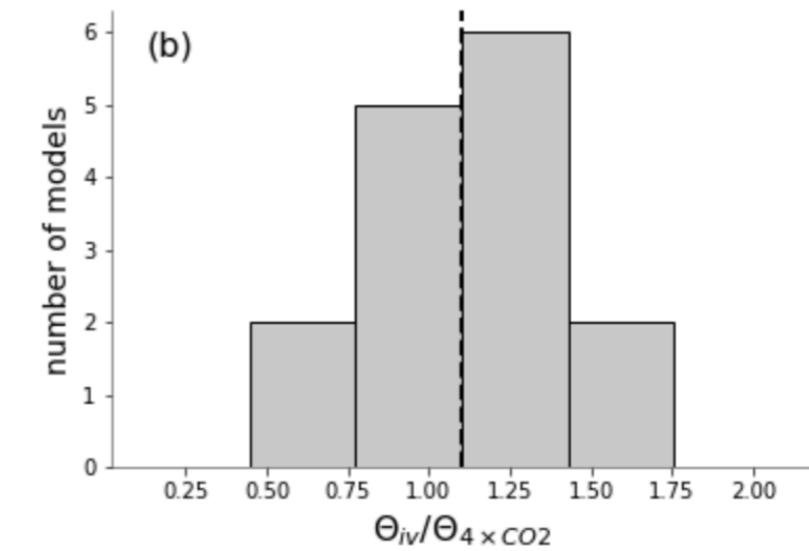
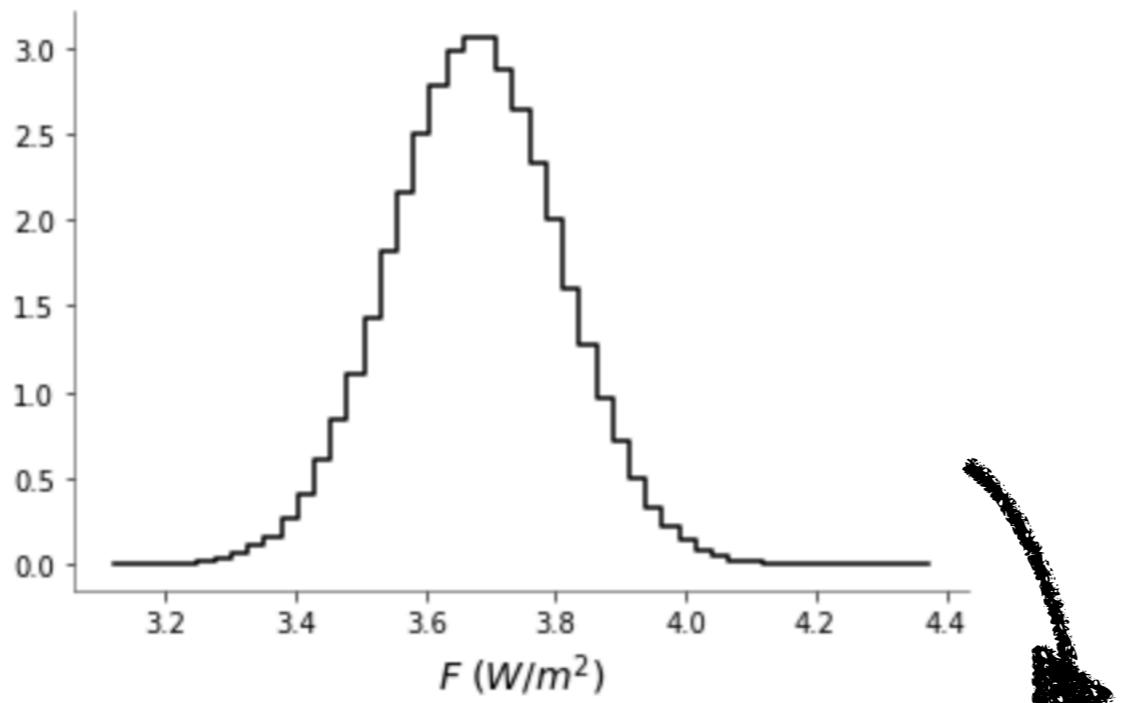
$$\text{ECS} \approx -\frac{F_{2\times CO_2}}{\Theta_{iv,obs}} \left( \frac{\Theta_{iv}}{\Theta_{4\times CO_2}} \right) \left( \frac{\Delta T_S}{\Delta T_A} \right)$$

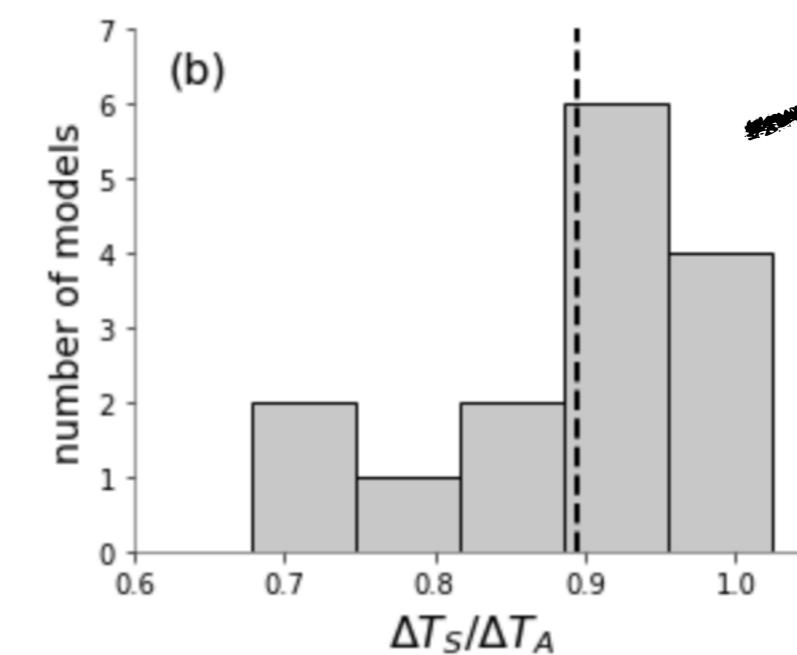
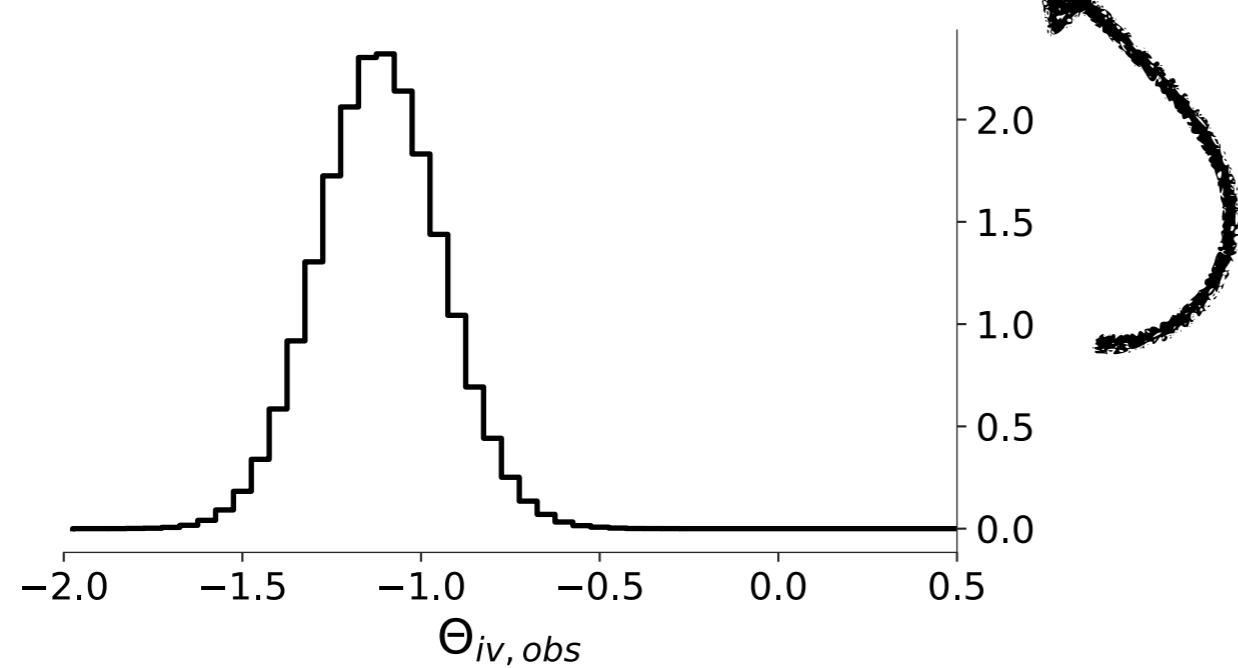
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**ATM**

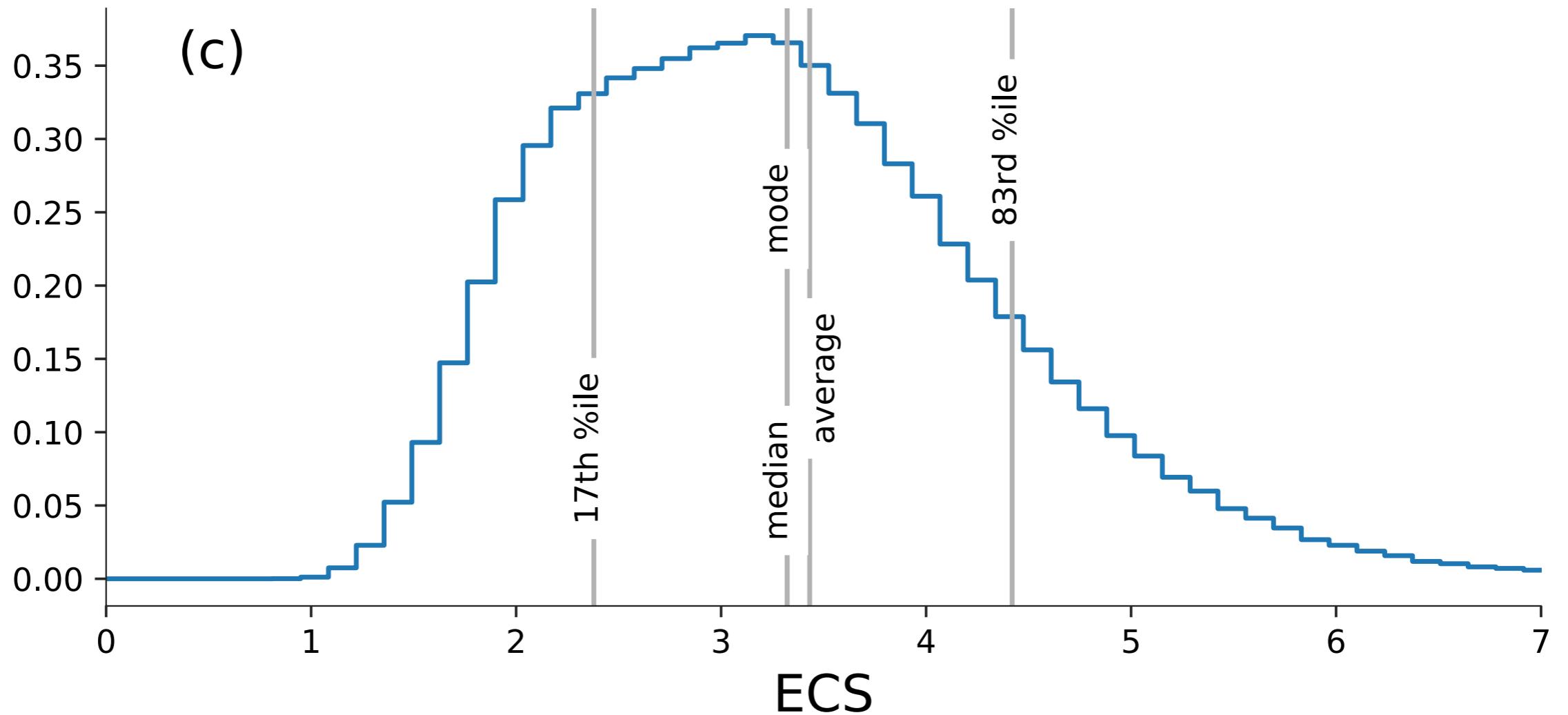


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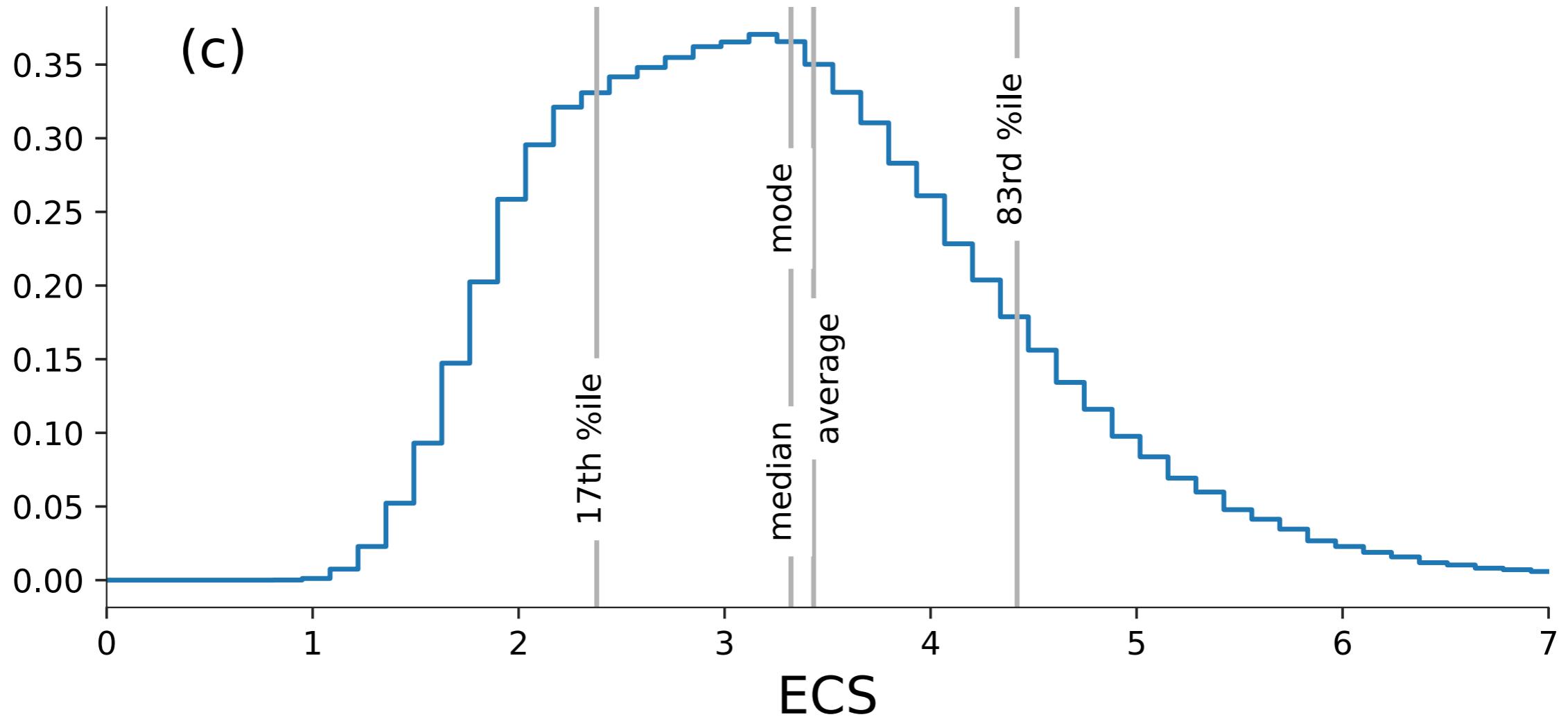


**ATM**

# ECS

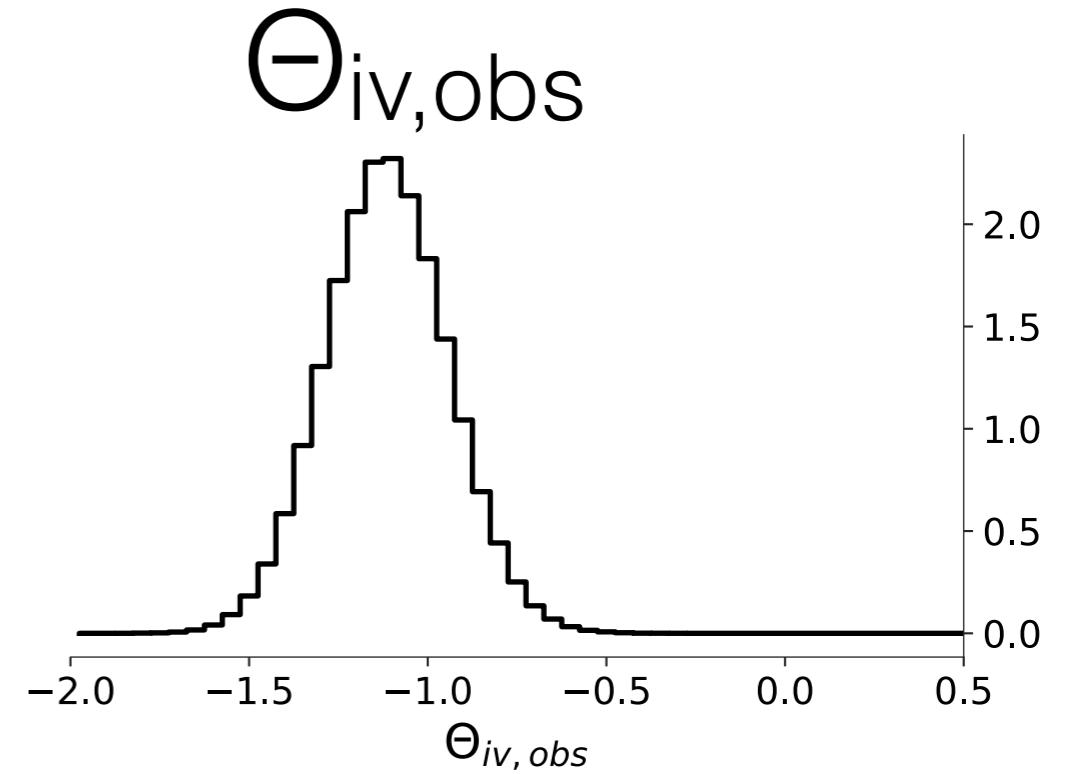
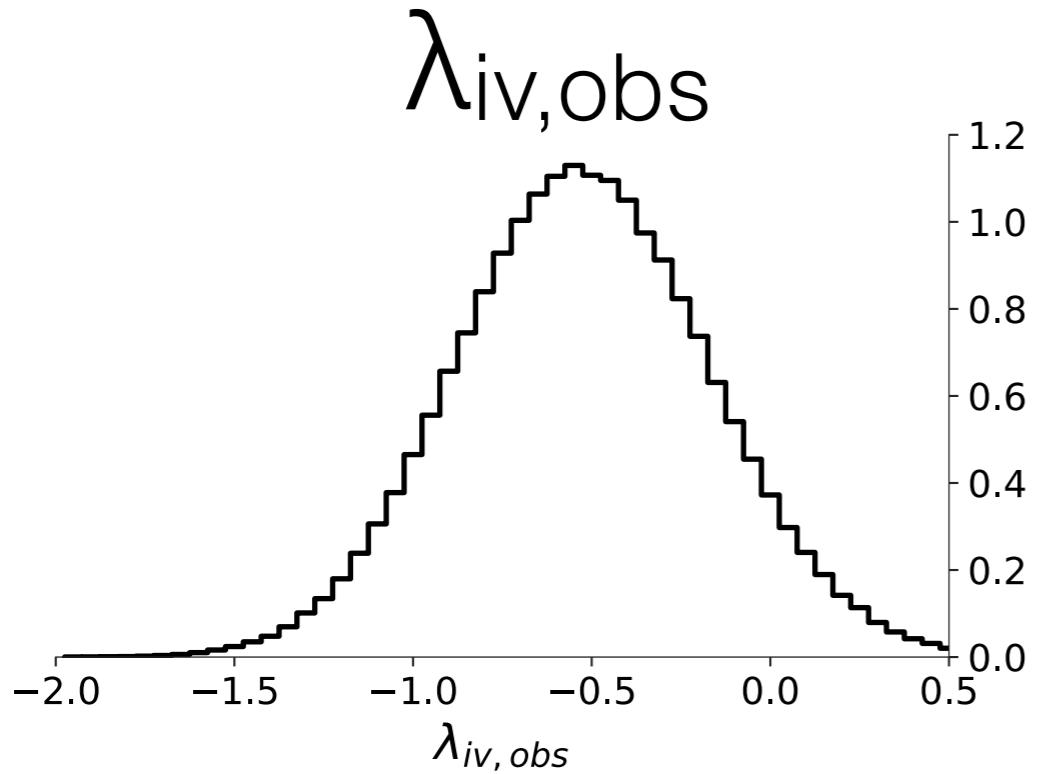


# ECS



*likely range: 2.4-4.5 K*  
median: 3.3 K





Also,  $\lambda_{iv}$  has larger interdecadal variability  
than  $\Theta_{iv}$

$$\text{ECS} \approx -\frac{F_{2\times CO_2}}{\Theta_{iv,obs}} \left( \frac{\Theta_{iv}}{\Theta_{4\times CO_2}} \right) \left( \frac{\Delta T_S}{\Delta T_A} \right)$$

$$\text{ECS} \approx -\frac{F_{2\times CO_2}}{\Theta_{iv,obs}} \left( \frac{\Theta_{iv}}{\Theta_{4\times CO_2}} \right) \left( \frac{\Delta T_S}{\Delta T_A} \right)$$

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40%

$$\text{ECS} \approx -\frac{F_{2\times CO_2}}{\Theta_{iv,obs}} \left( \frac{\Theta_{iv}}{\Theta_{4\times CO_2}} \right) \left( \frac{\Delta T_S}{\Delta T_A} \right)$$

40%

We can compare  $\Theta_{iv}$  in the models to observations

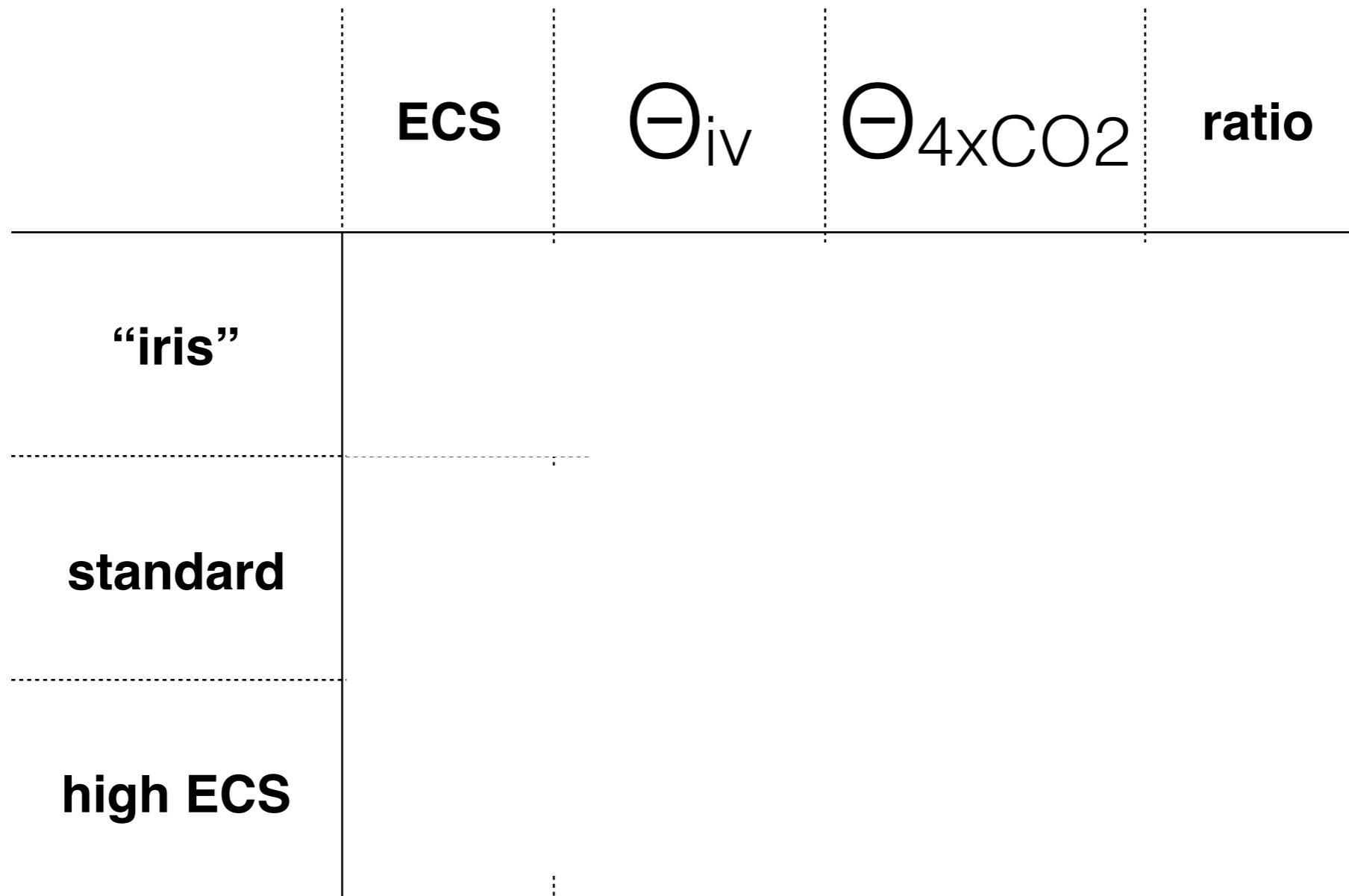
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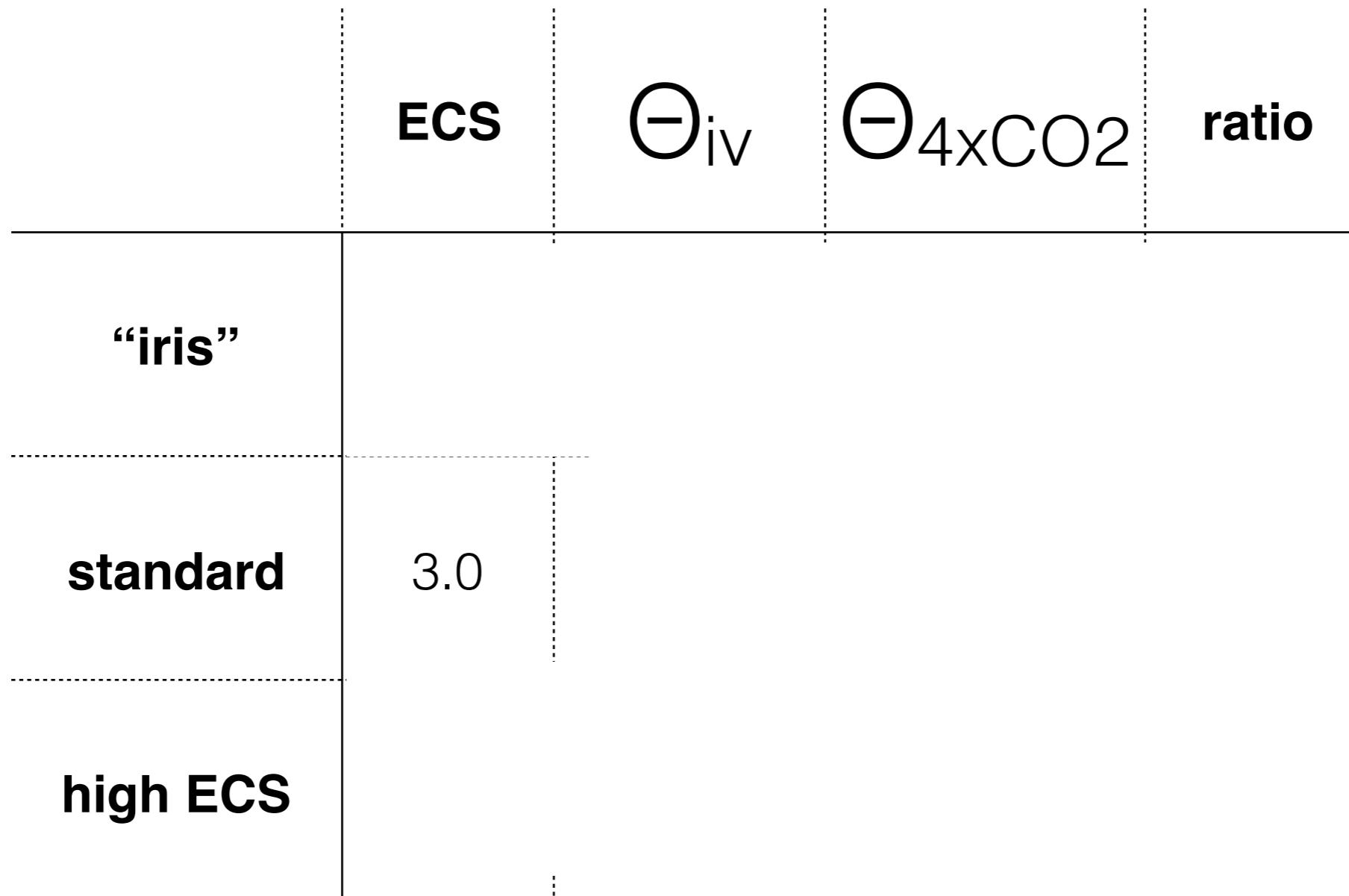
... error in ratio requires error in numerator that is not reflected in the denominator ...

# Test with MPI-ESM 1.2



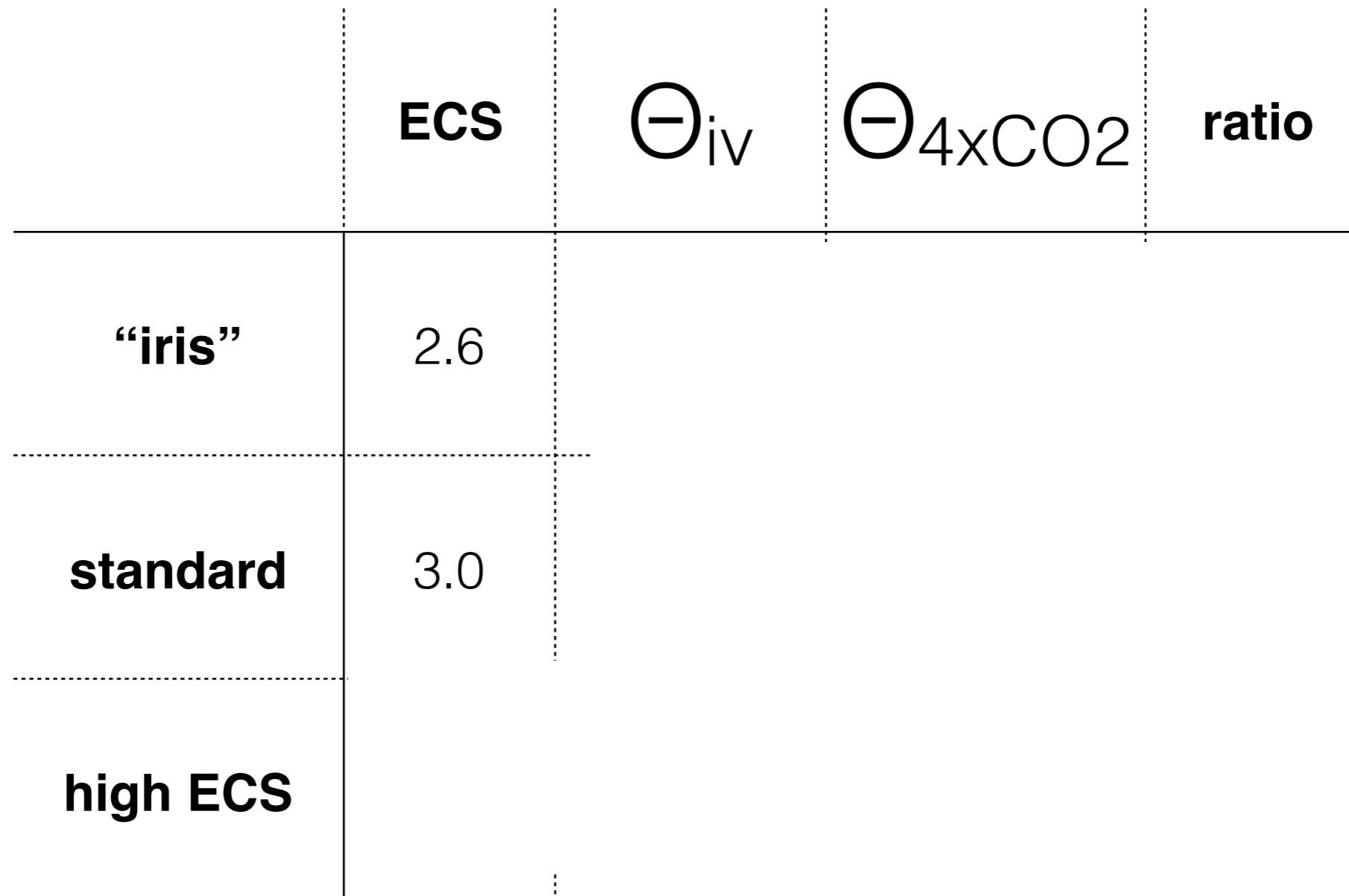
Thanks to T. Mauritsen and D. Jimenez for the model runs

# Test with MPI-ESM 1.2



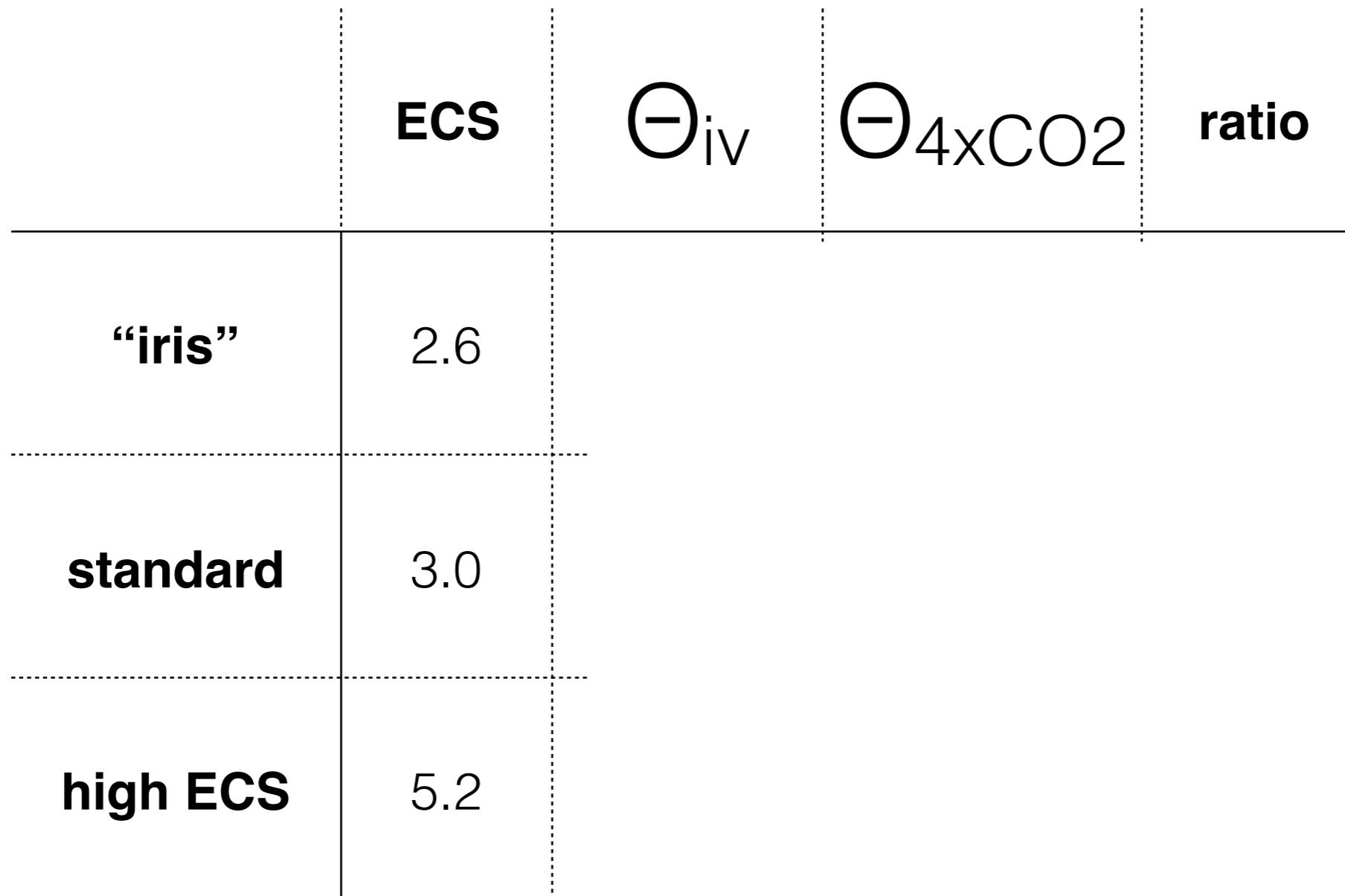
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# Test with MPI-ESM 1.2



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# Test with MPI-ESM 1.2

	ECS	$\Theta_{\text{iv}}$	$\Theta_{4\times\text{CO}_2}$	ratio
“iris”	2.6	-1.29		
standard	3.0	-0.98		
high ECS	5.2	-0.57		

Thanks to T. Mauritsen and D. Jimenez for the model runs

# Test with MPI-ESM 1.2

	ECS	$\Theta_{\text{iv}}$	$\Theta_{4\times\text{CO}_2}$	ratio
“iris”	2.6	-1.29	-1.23	
standard	3.0	-0.98	-1.04	
high ECS	5.2	-0.57	-0.63	

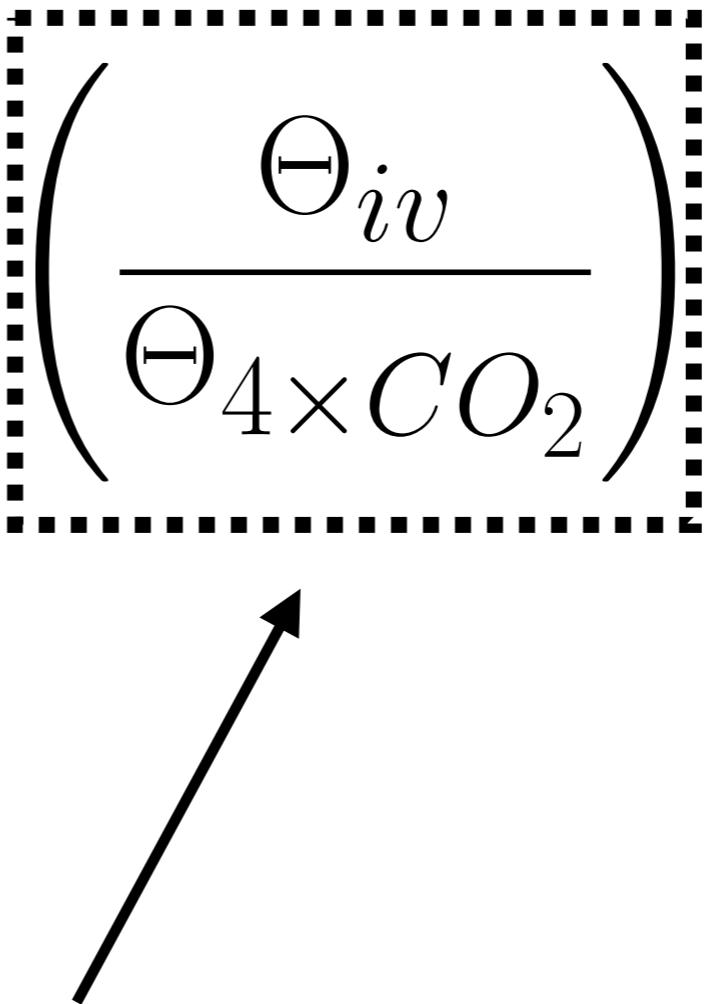
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# Test with MPI-ESM 1.2

	ECS	$\Theta_{\text{iv}}$	$\Theta_{4\times\text{CO}_2}$	ratio
“iris”	2.6	-1.29	-1.23	0.96
standard	3.0	-0.98	-1.04	1.06
high ECS	5.2	-0.57	-0.63	1.10

Thanks to T. Mauritsen and D. Jimenez for the model runs

$$\text{ECS} \approx -\frac{F_{2\times CO_2}}{\Theta_{iv,obs}} \left( \frac{\Theta_{iv}}{\Theta_{4\times CO_2}} \right) \left( \frac{\Delta T_S}{\Delta T_A} \right)$$

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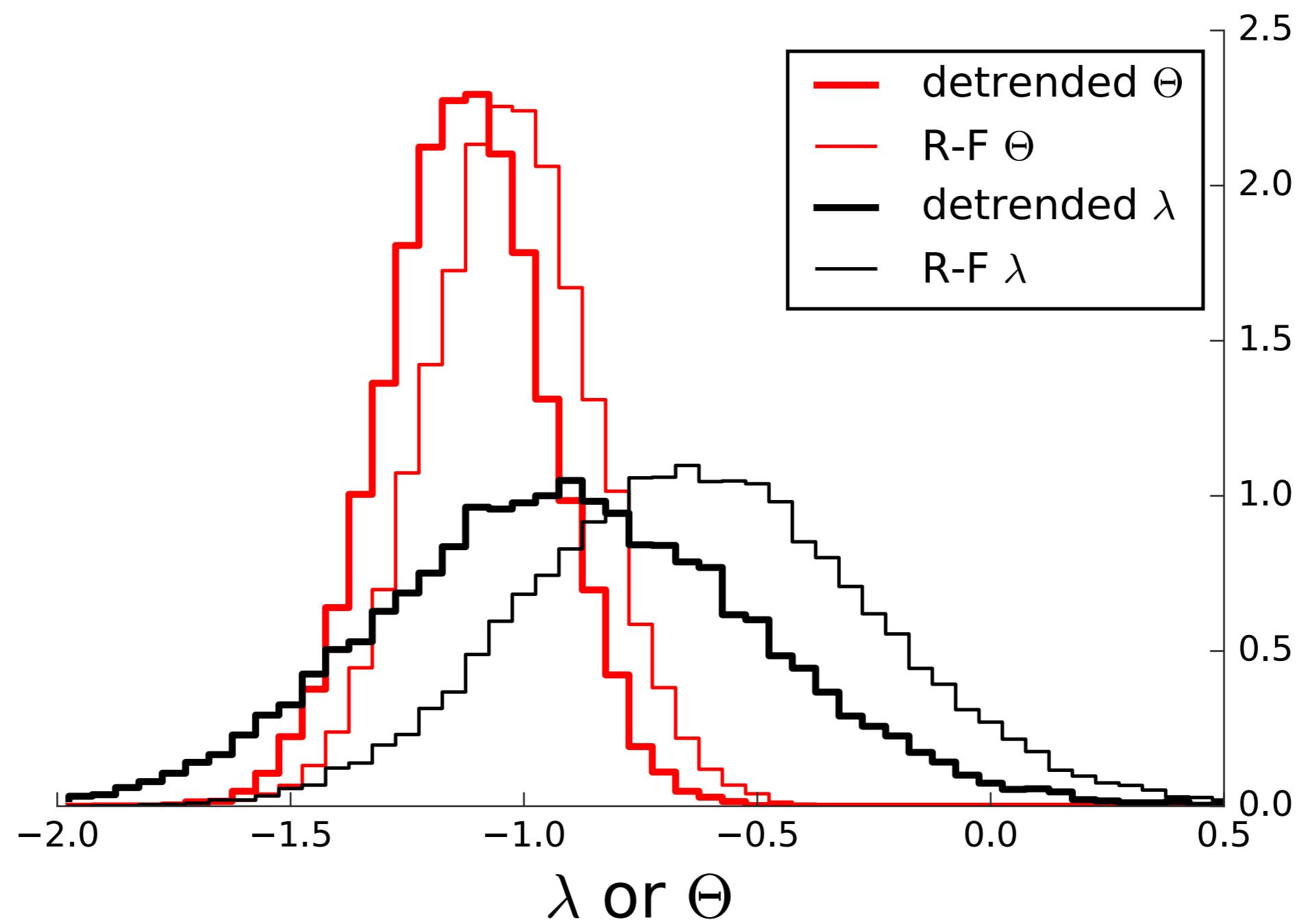
This is a believable model-derived quantity

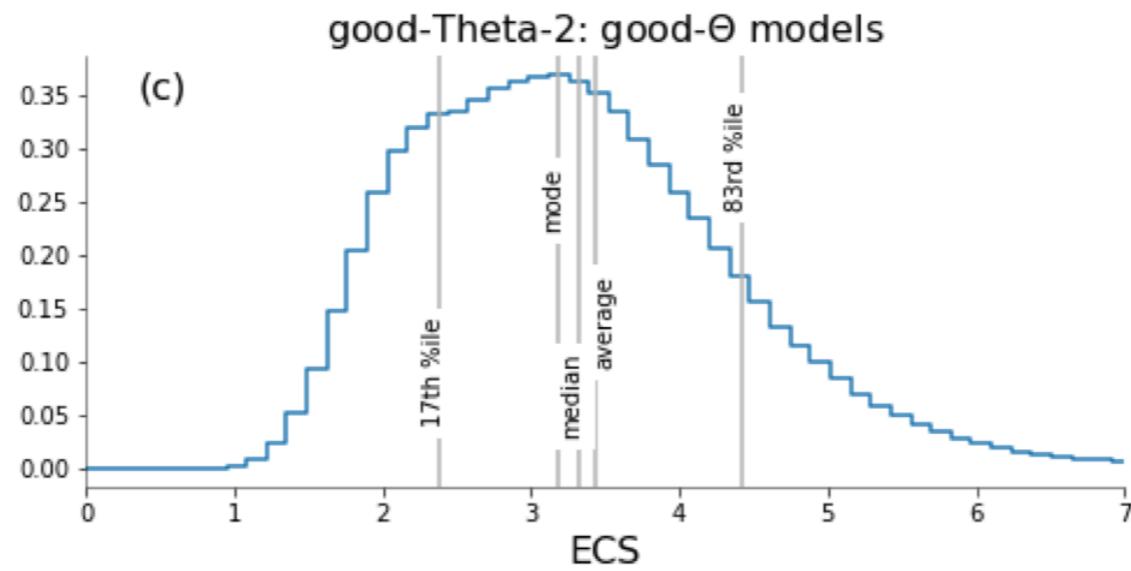
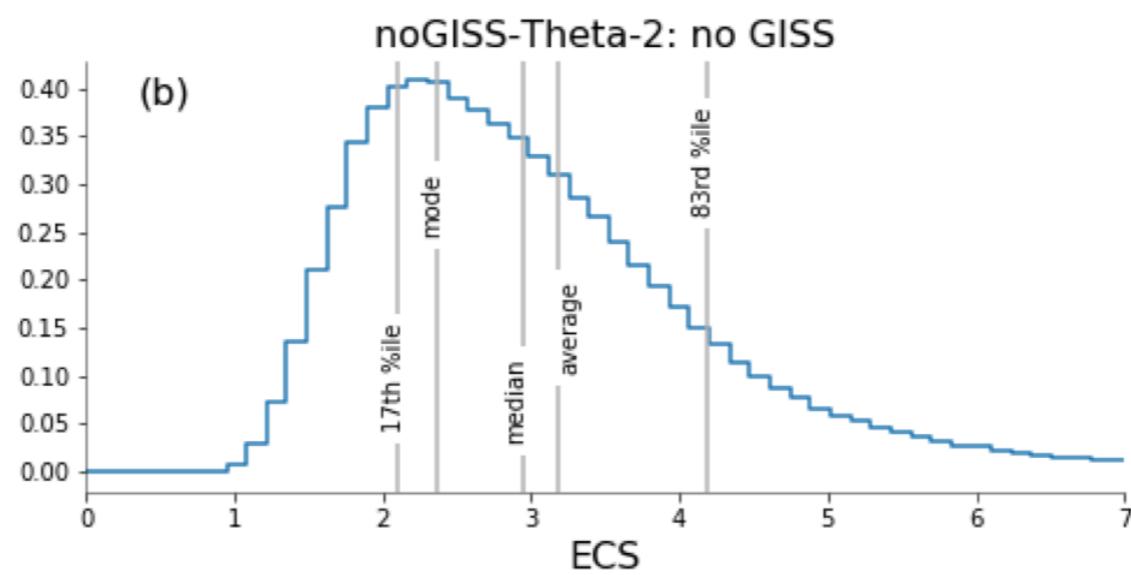
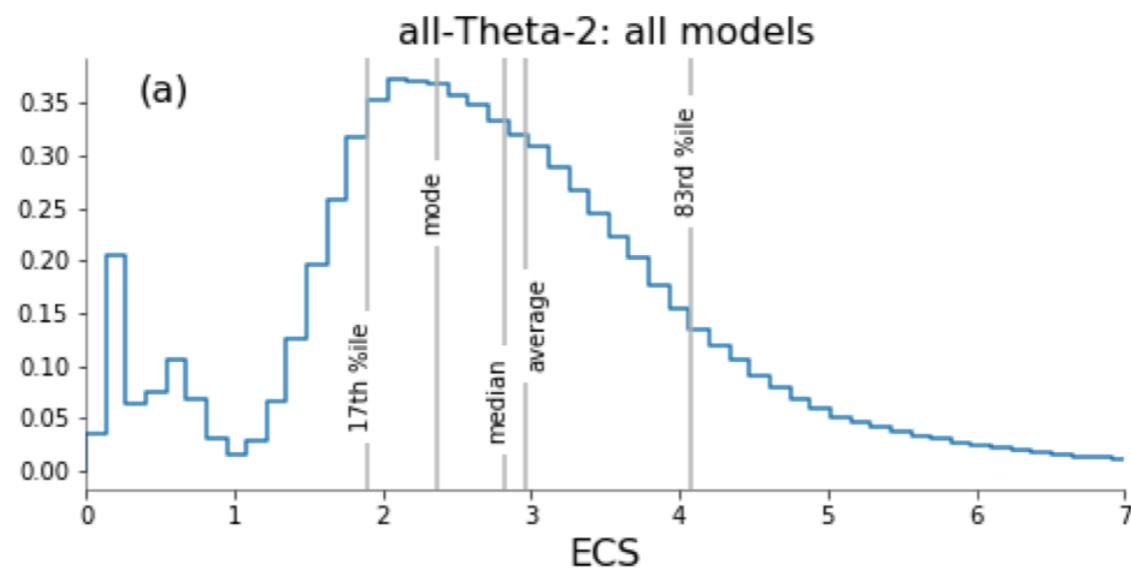
# Conclusions

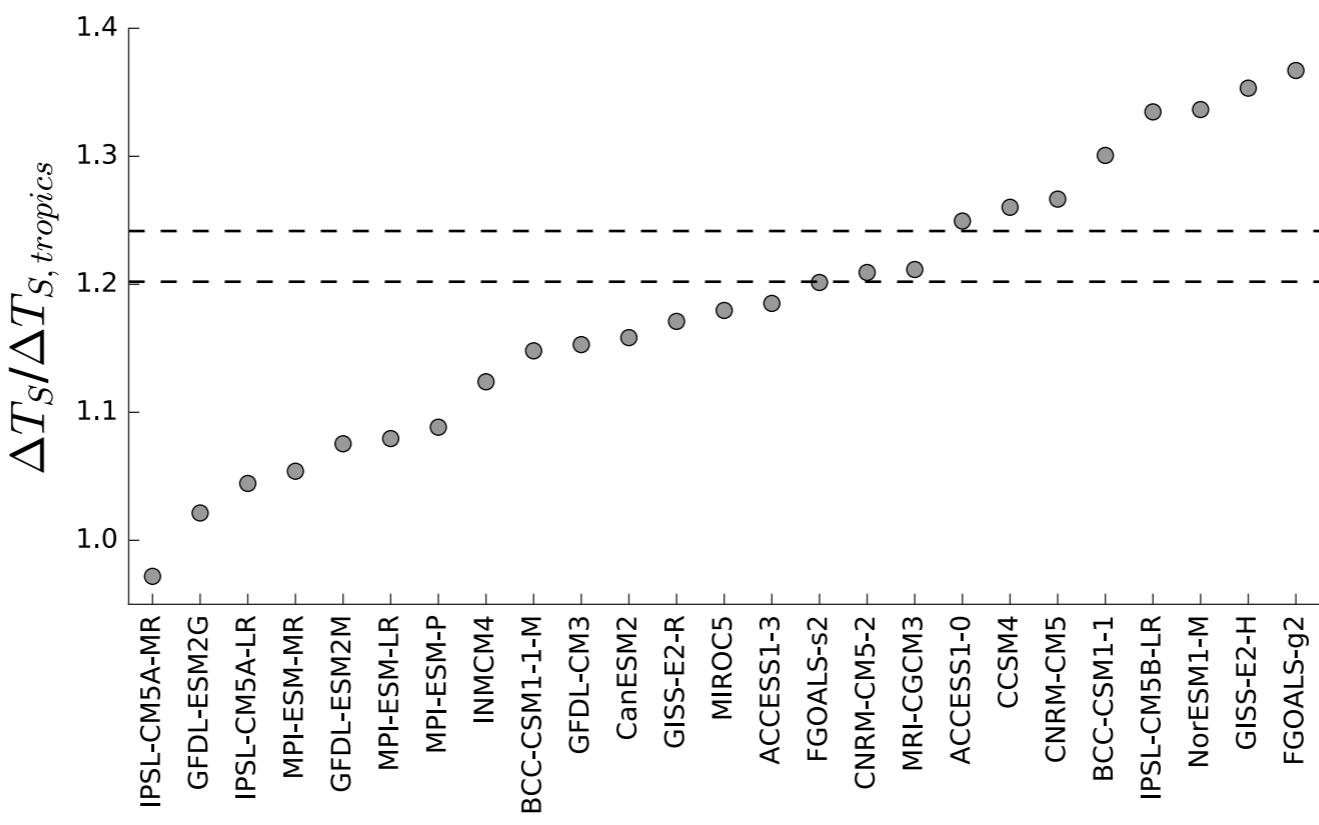
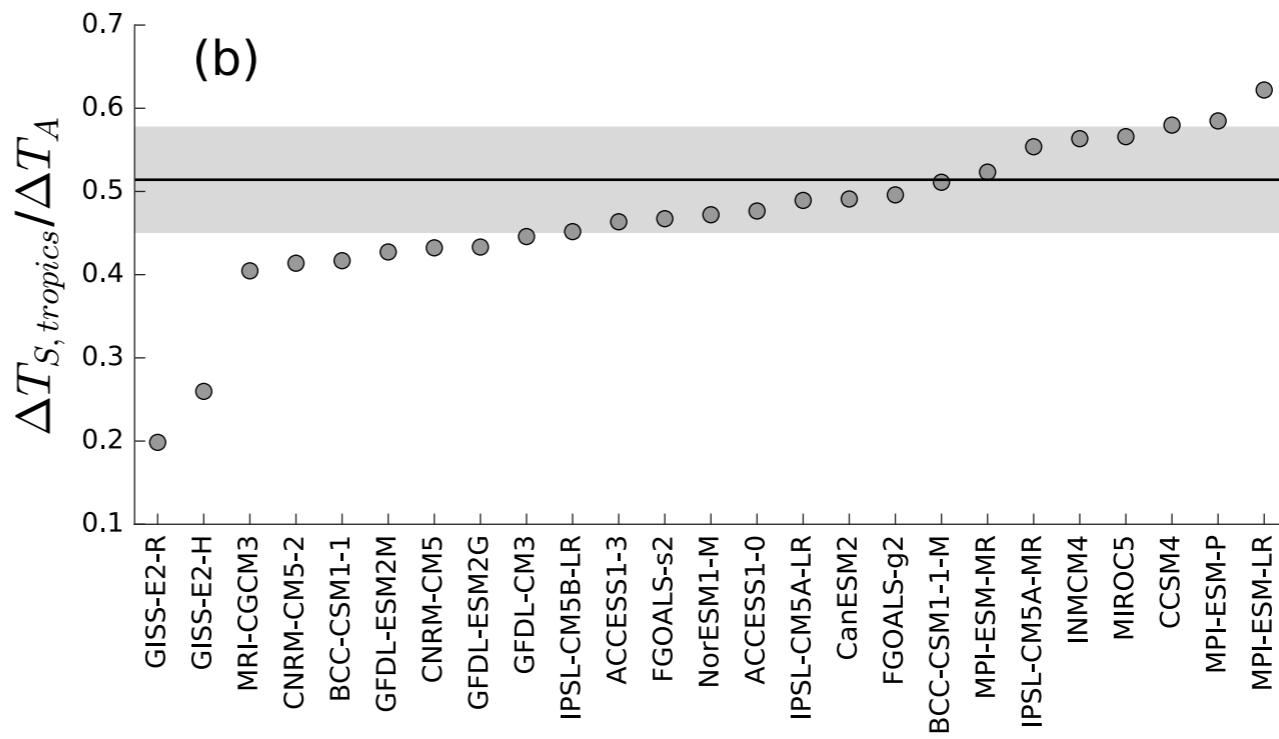
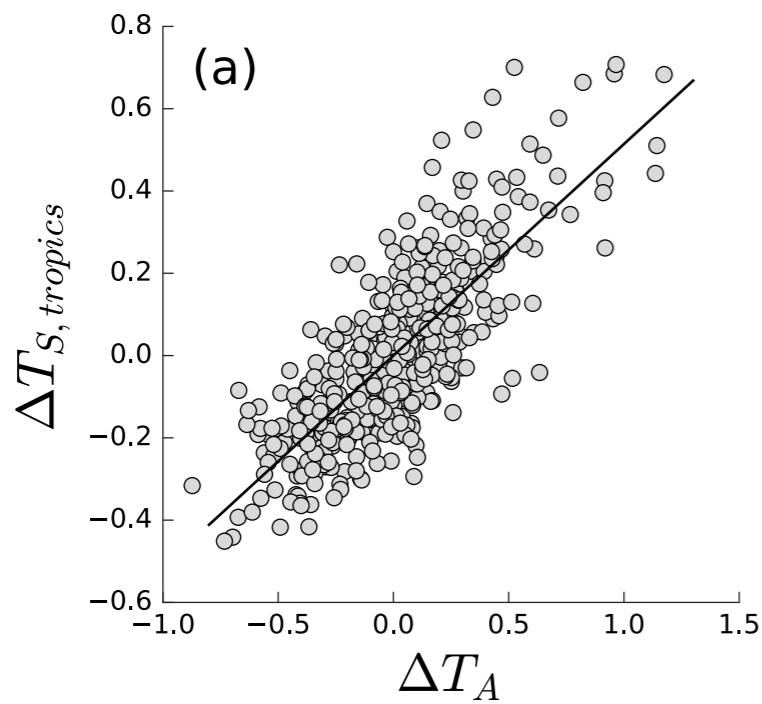
- Using interannual variability, we estimate ECS is *likely* 2.4-4.5 K
- We see no evidence of low ECS (1.5-2 K) suggested by estimates based on the 20th century record
- Key parameter is the ratio  $\Theta_{\text{iv}}/\Theta_{4\times\text{CO}_2}$
- Pre-print: <https://eartharxiv.org/4et67/>



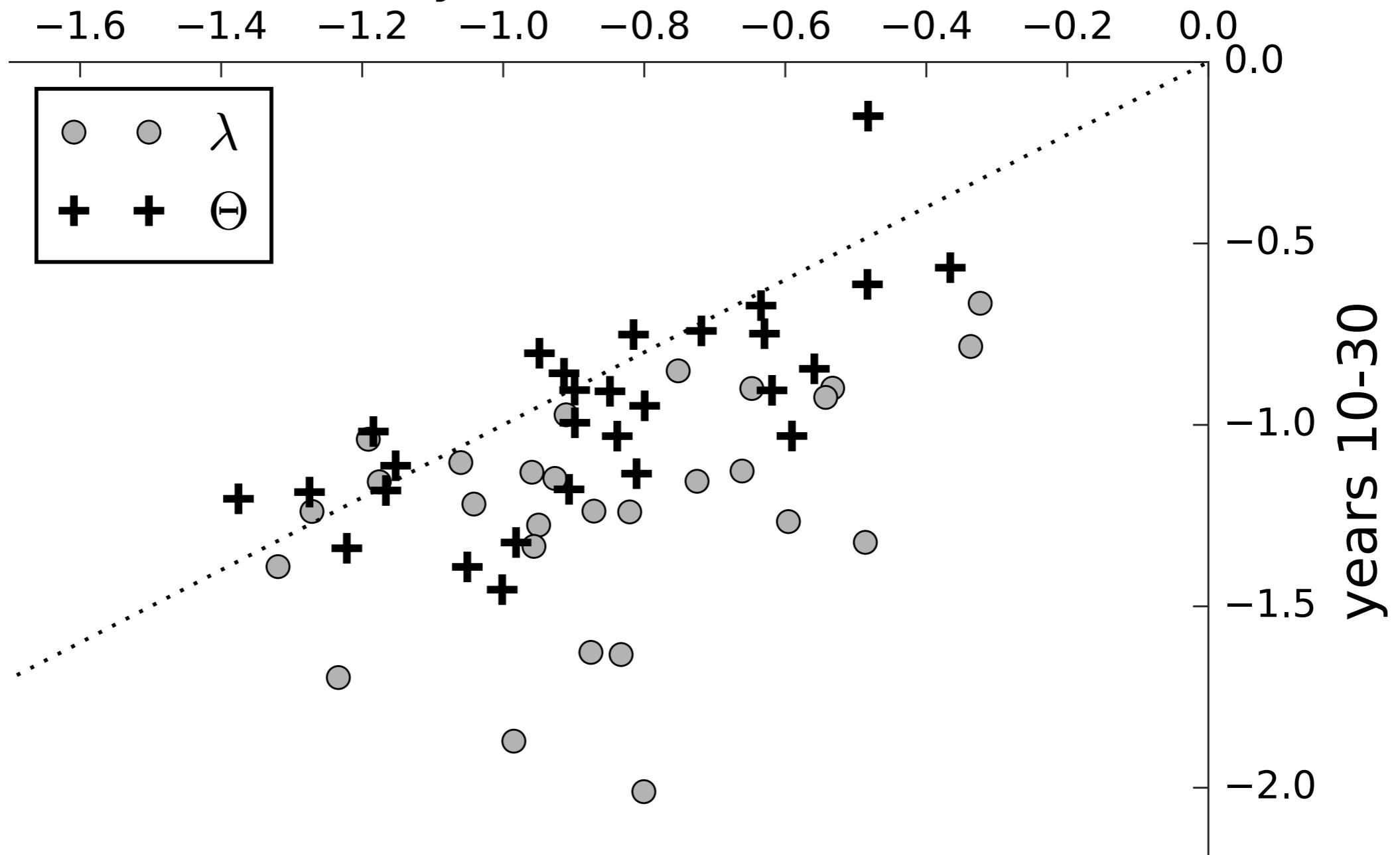
# backup slides

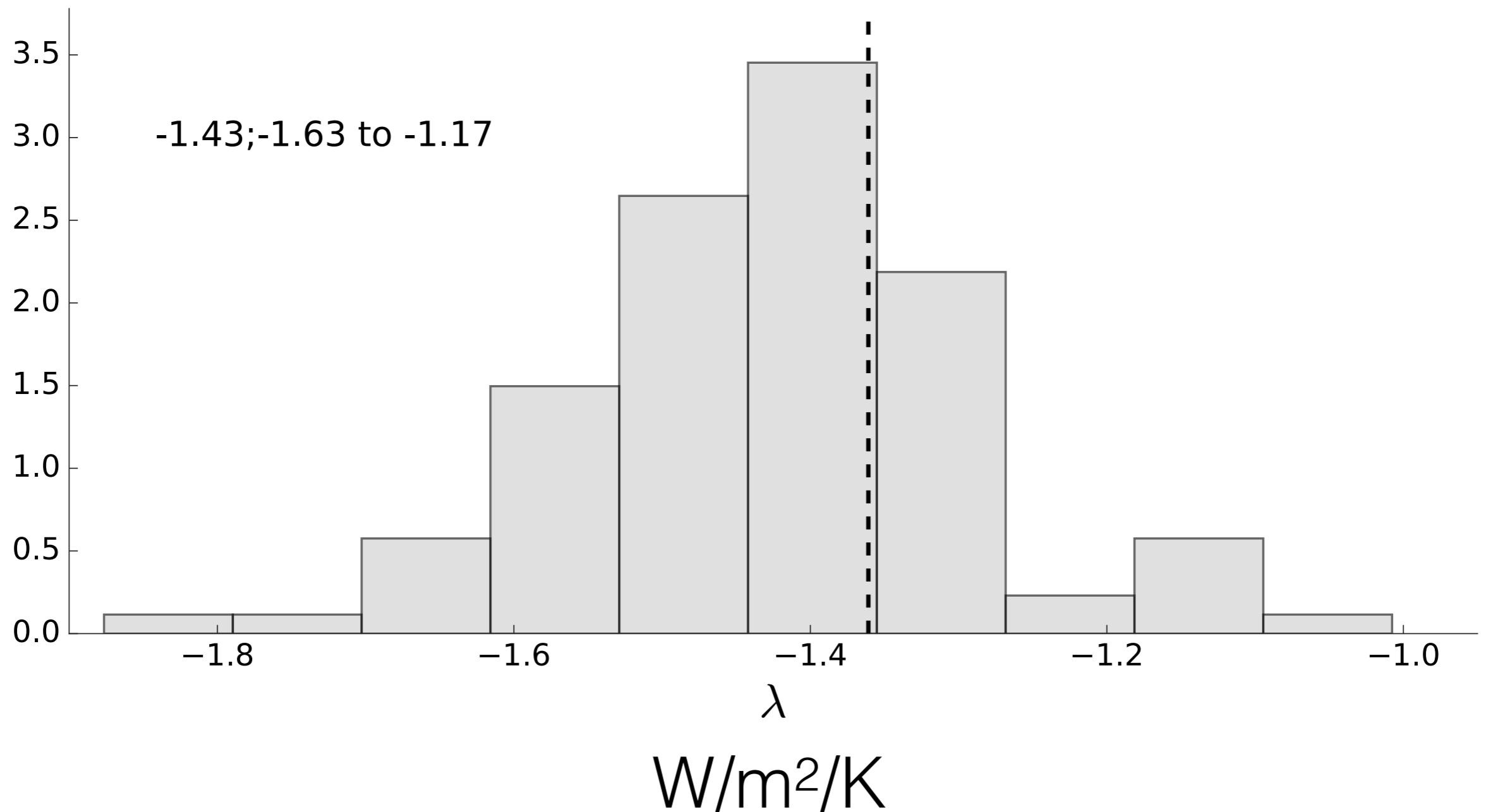




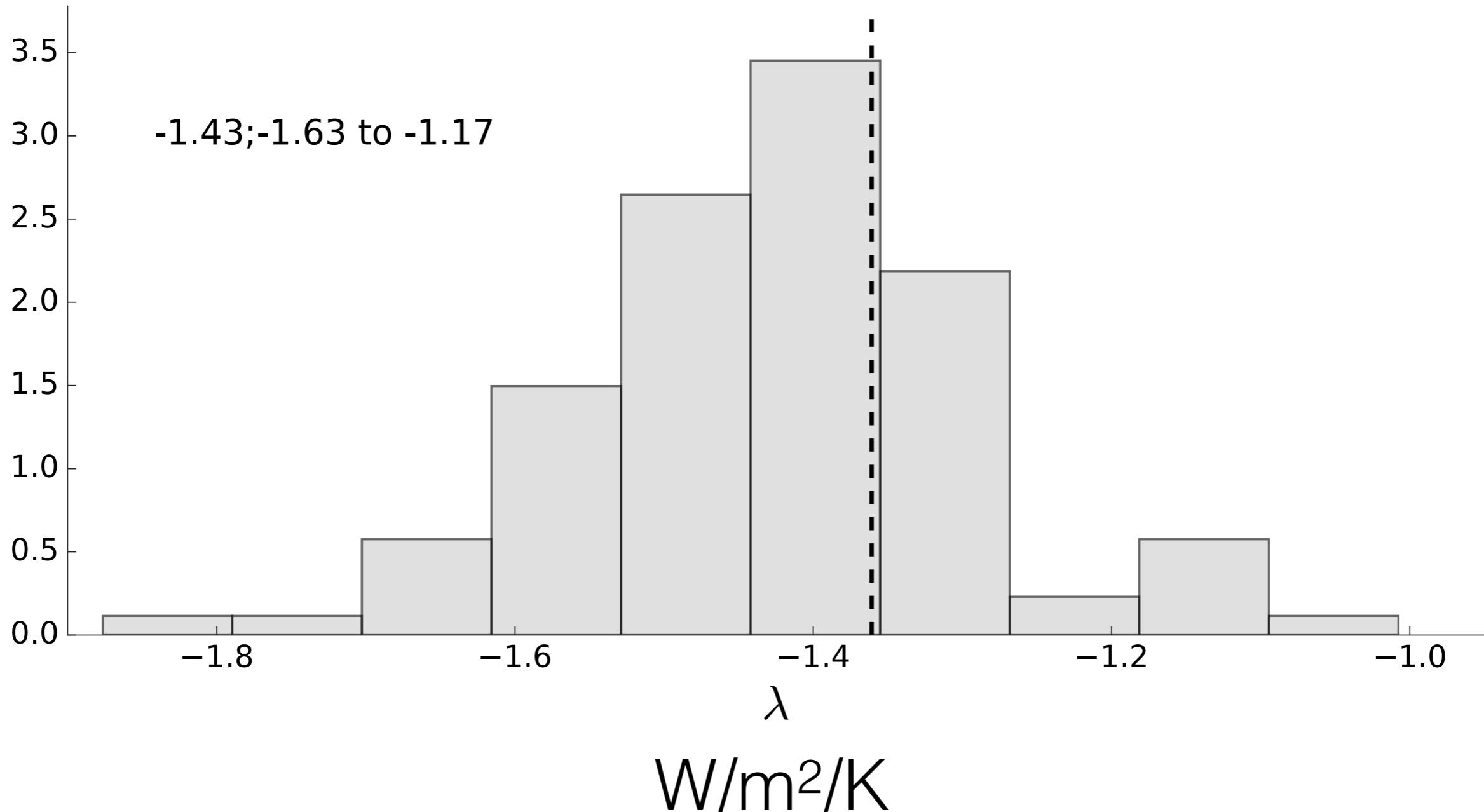


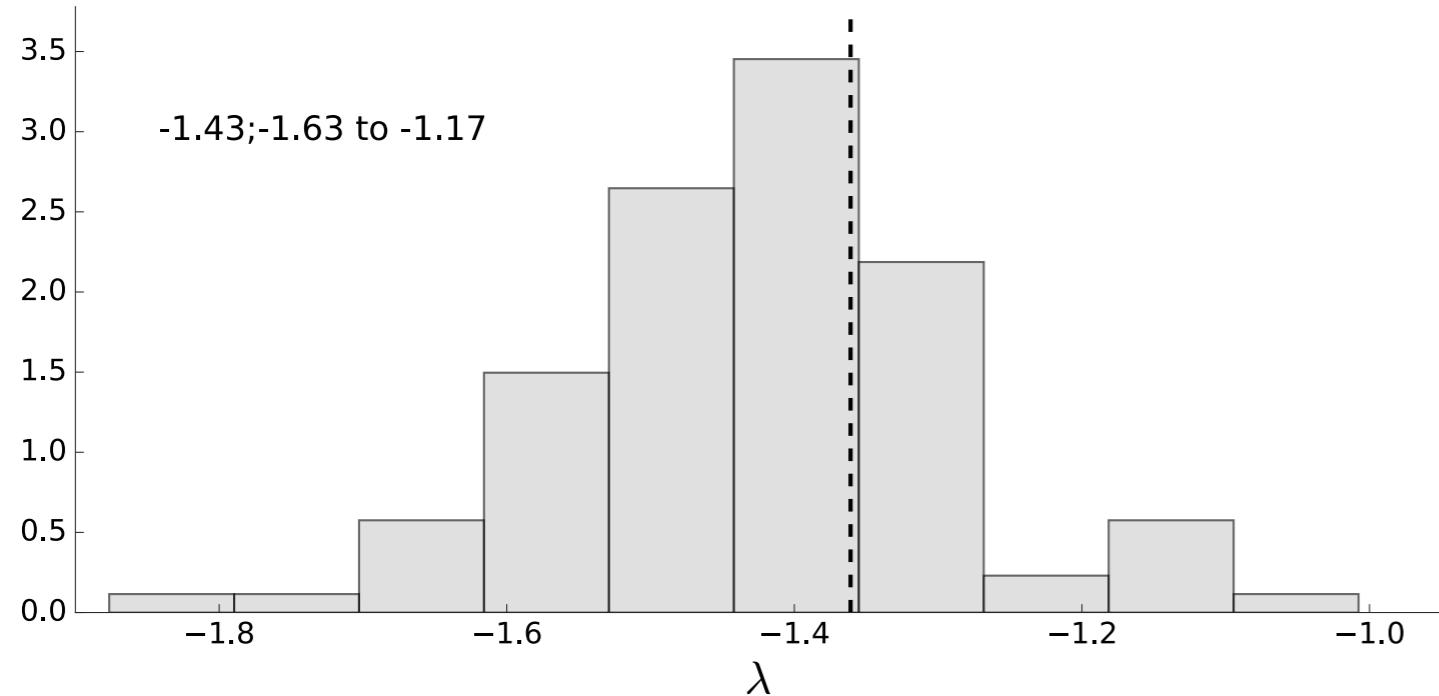
years 30-150





# internal variability

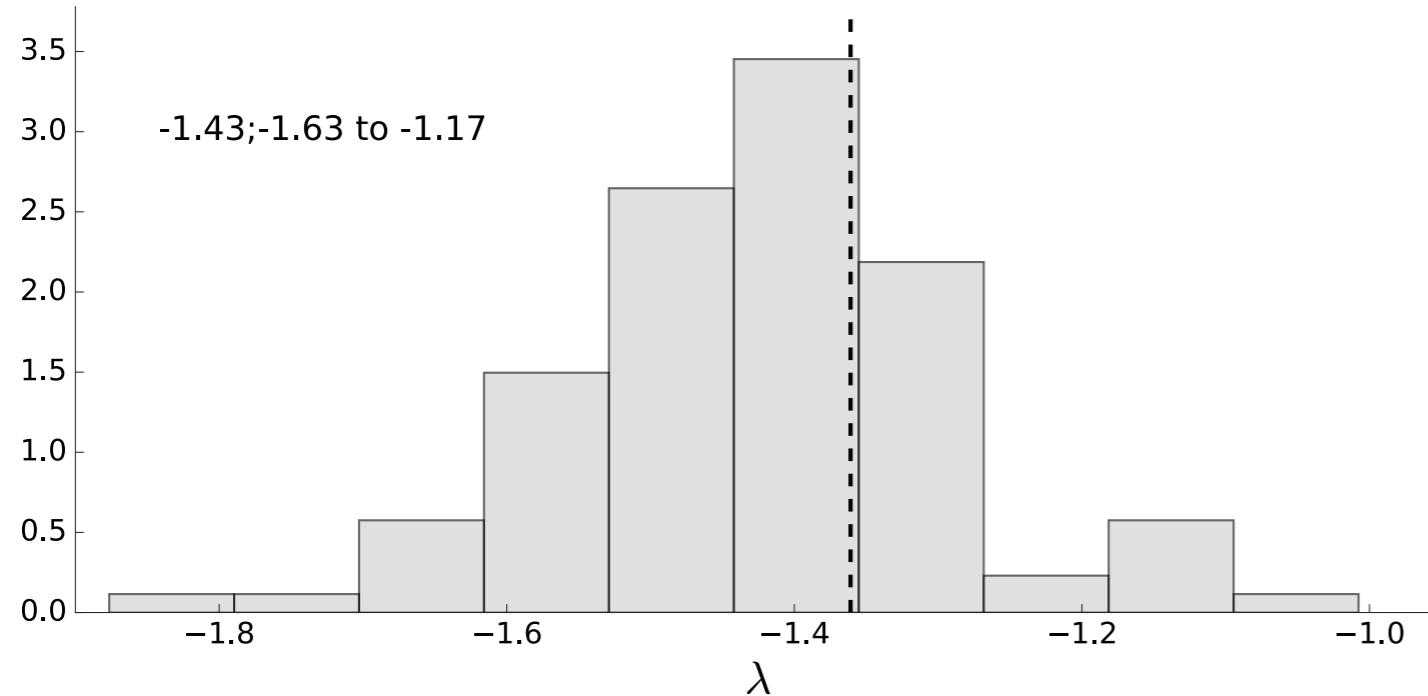




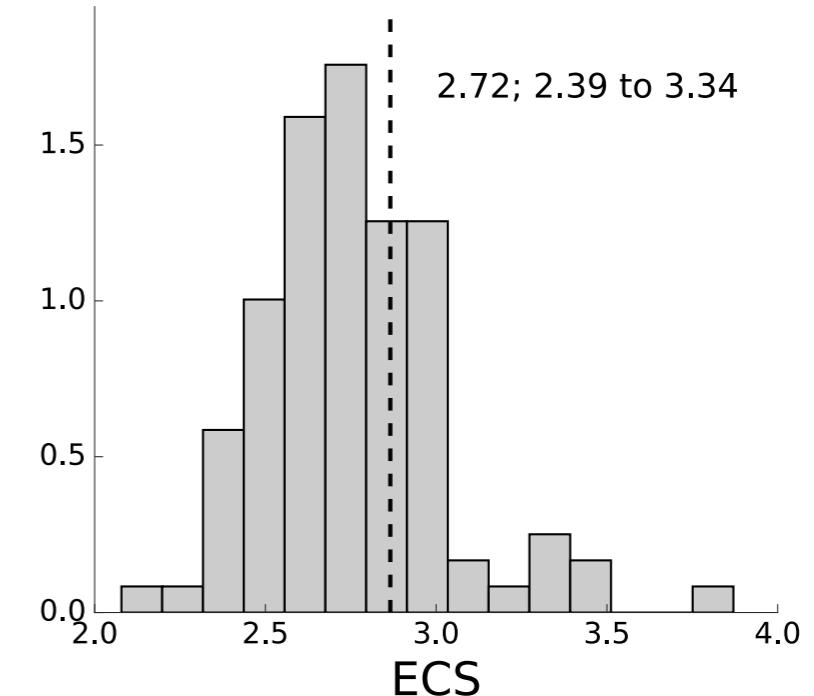
-1.43;-1.63 to -1.17

$$\lambda = \frac{\Delta(R - F)}{\Delta T_S}$$

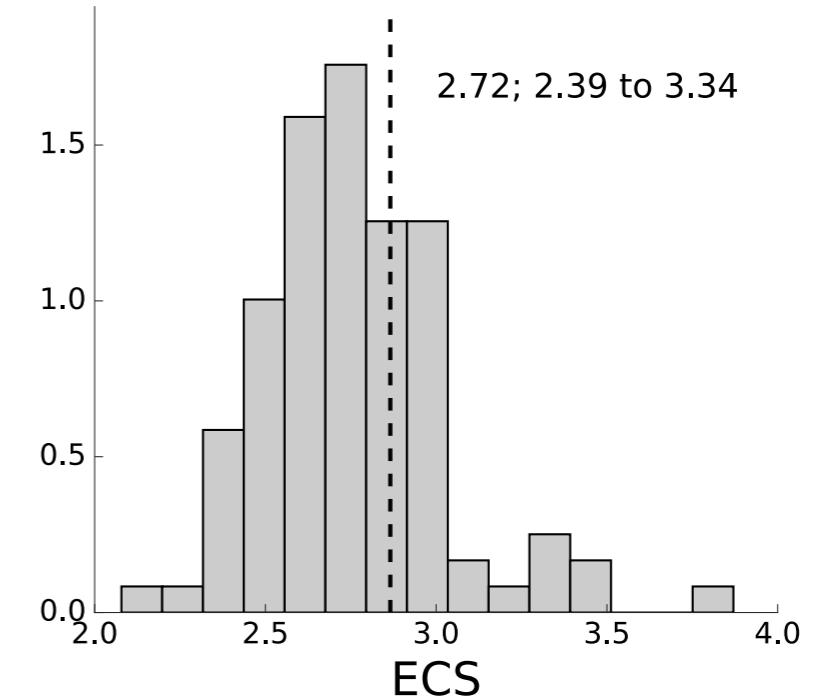
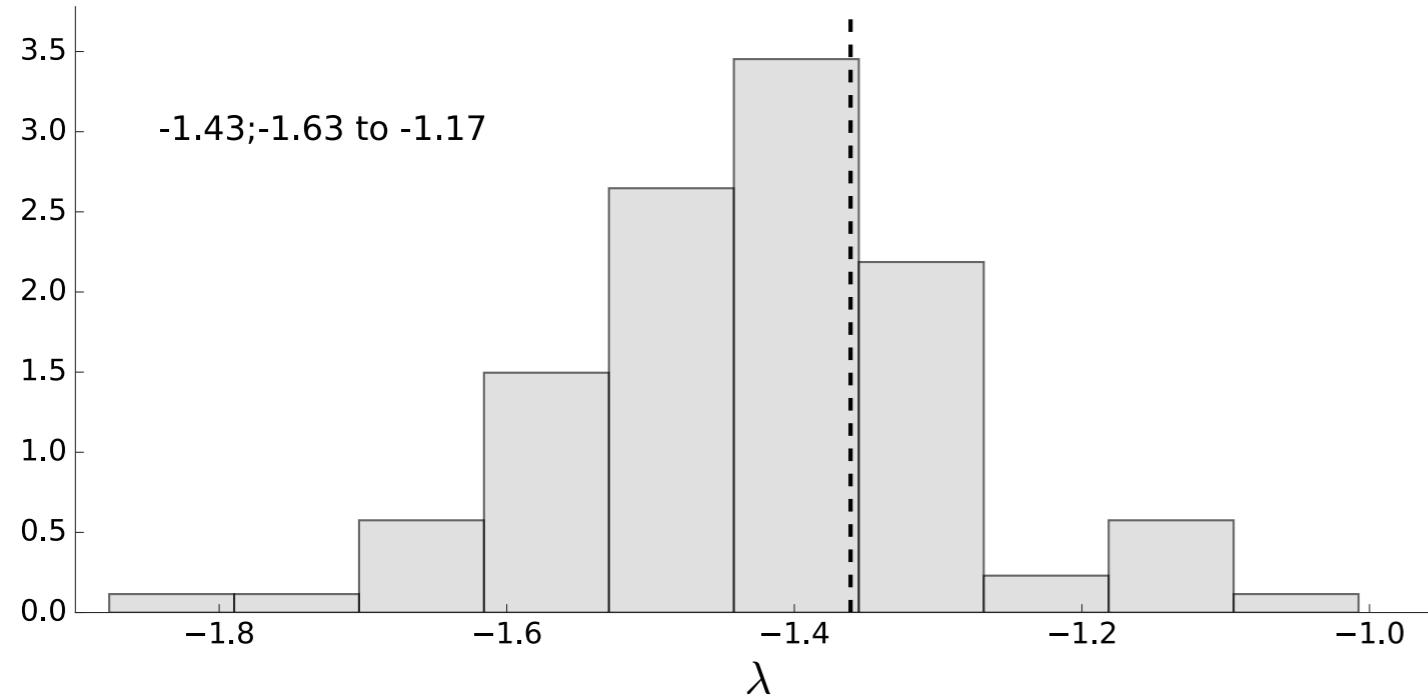
$$\text{ECS} = -\frac{F_{2\times CO_2}}{\lambda}$$

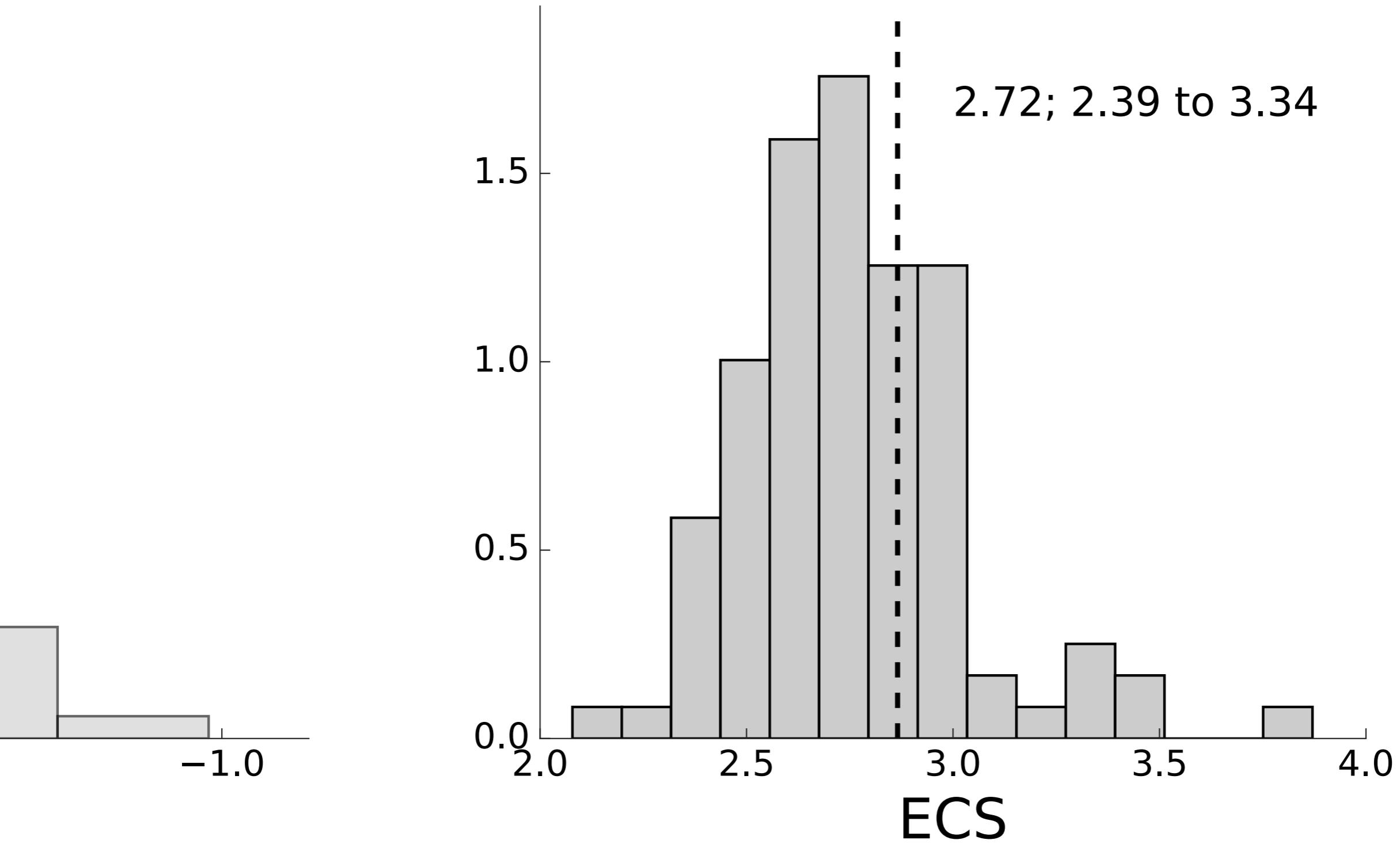


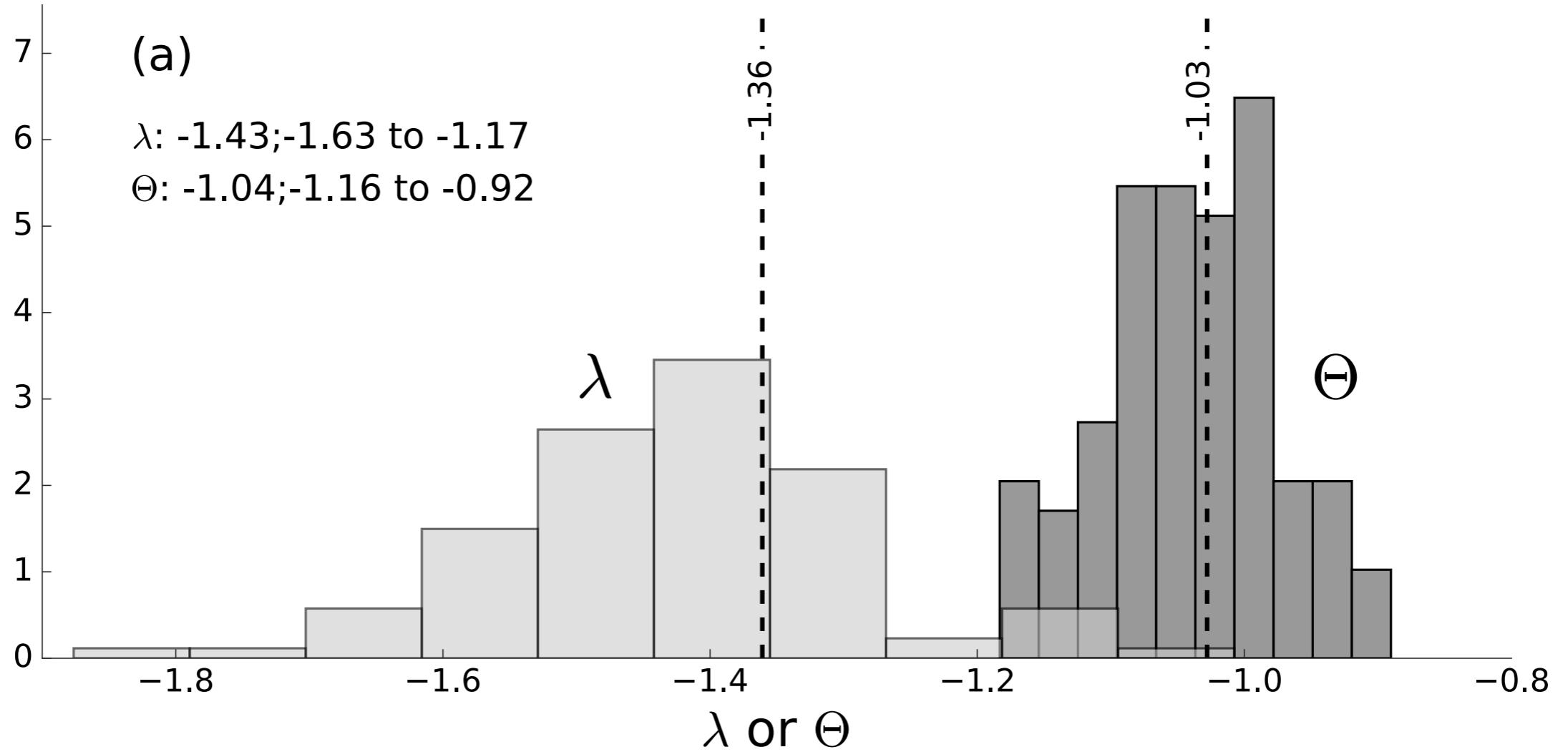
$$\lambda = \frac{\Delta(R - F)}{\Delta T_S}$$



$$ECS = -\frac{F_{2\times CO_2}}{\lambda}$$

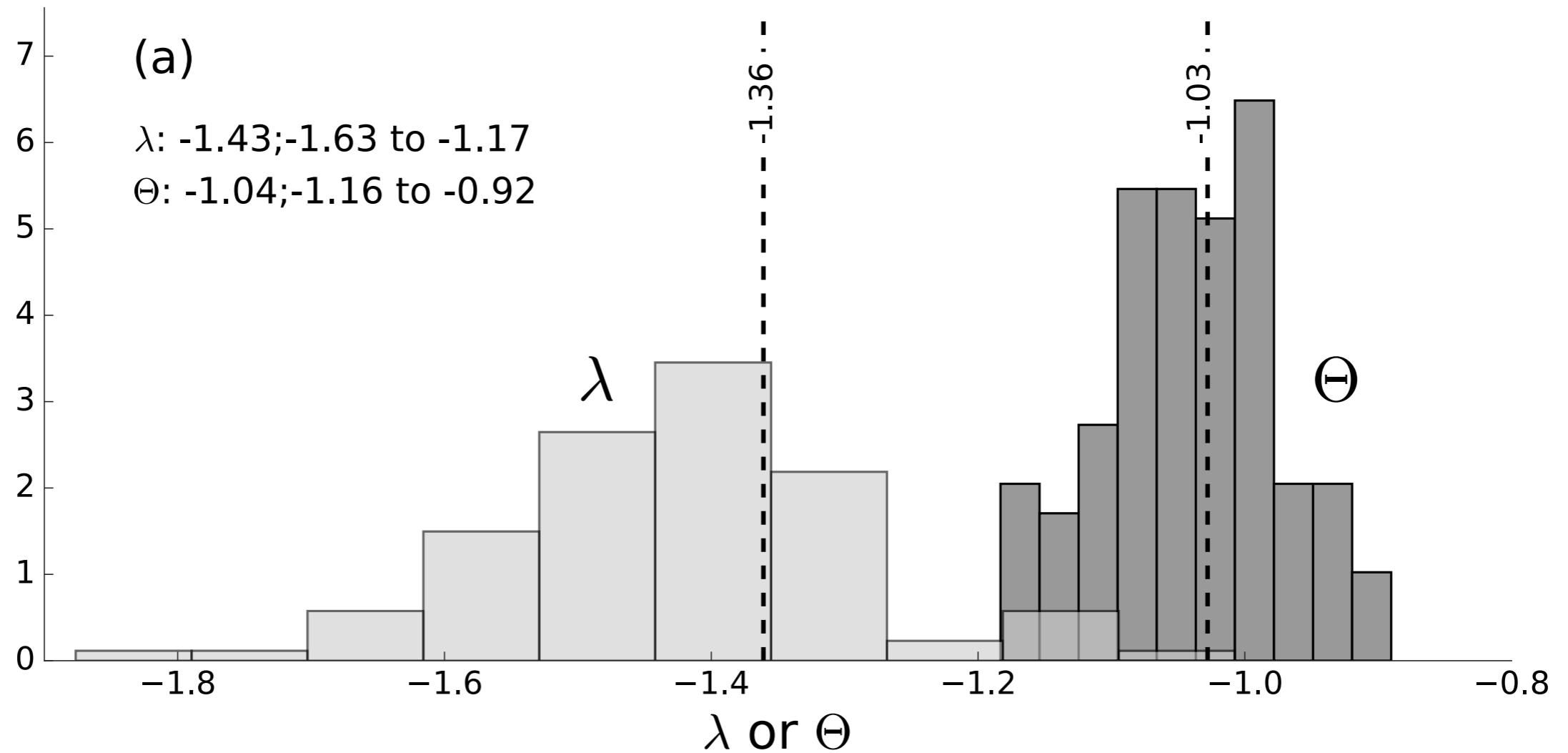






$$\lambda = \Delta(R-F)/\Delta T_S$$

$$\Theta = \Delta(R-F)/\Delta T_A$$



$$\lambda = \Delta(R-F)/\Delta T_S$$

$$\Theta = \Delta(R-F)/\Delta T_A$$

Table 1. ECS values from the  $\lambda$  runs

Summary of the statistics of the ECS distributions derived using Eq. 4. “%<2” and “%>4.5” gives the percent of ECS values that are below 2 K or above 4.5 K. Units are in K, except for “%<2” and “%>4.5”, which are in percent.

<b>run</b>	<b>mean</b>	<b>mode</b>	<b>median</b>	<b>5-95%</b>	<b>17-83%</b>	<b>%&lt;2</b>	<b>%&gt;4.5</b>
all-Lambda-1	4.63	2.98	4.23	1.7-8.8	2.5-7.0	6	32
all-Lambda-2	3.78	2.44	3.29	1.4-7.9	2.0-5.7	15	26
all-Lambda-1-f	4.43	2.71	3.99	1.6-8.7	2.3-6.7	8	30
all-Lambda-1-f_20-150	4.59	2.85	4.19	1.6-8.9	2.4-7.0	7	31
good-Lambda-1	4.20	2.71	3.73	1.6-8.4	2.3-6.3	9	28
good-Lambda-2	3.66	2.31	3.19	1.4-7.7	1.9-5.4	16	24
good-Lambda-1-f_20-150	4.18	2.71	3.72	1.4-8.5	2.2-6.4	10	28
good-Lambda-1-f	3.98	2.44	3.48	1.4-8.3	2.1-6.0	12	25

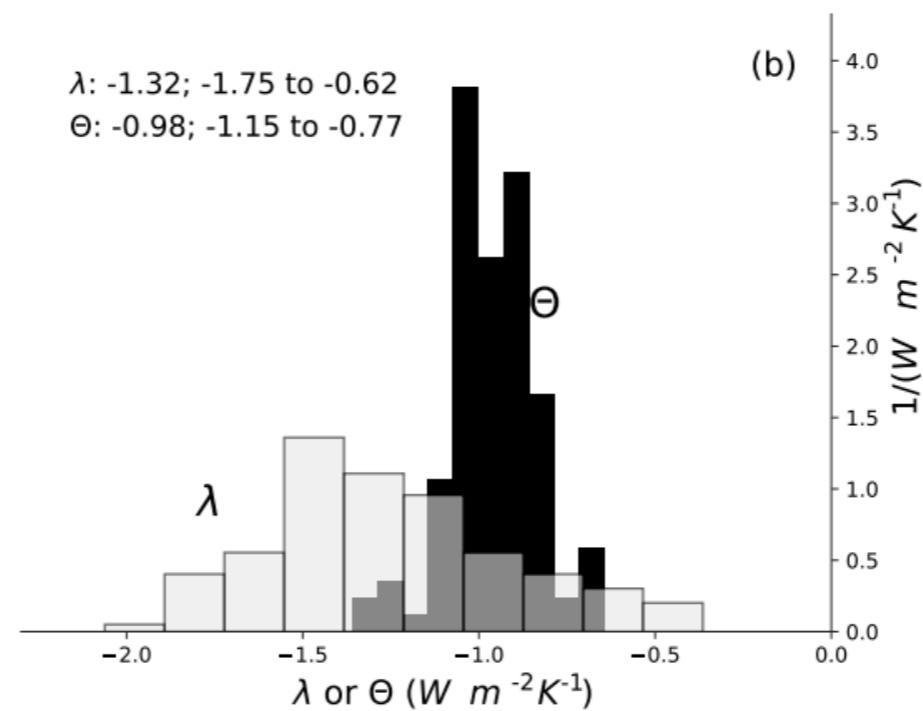
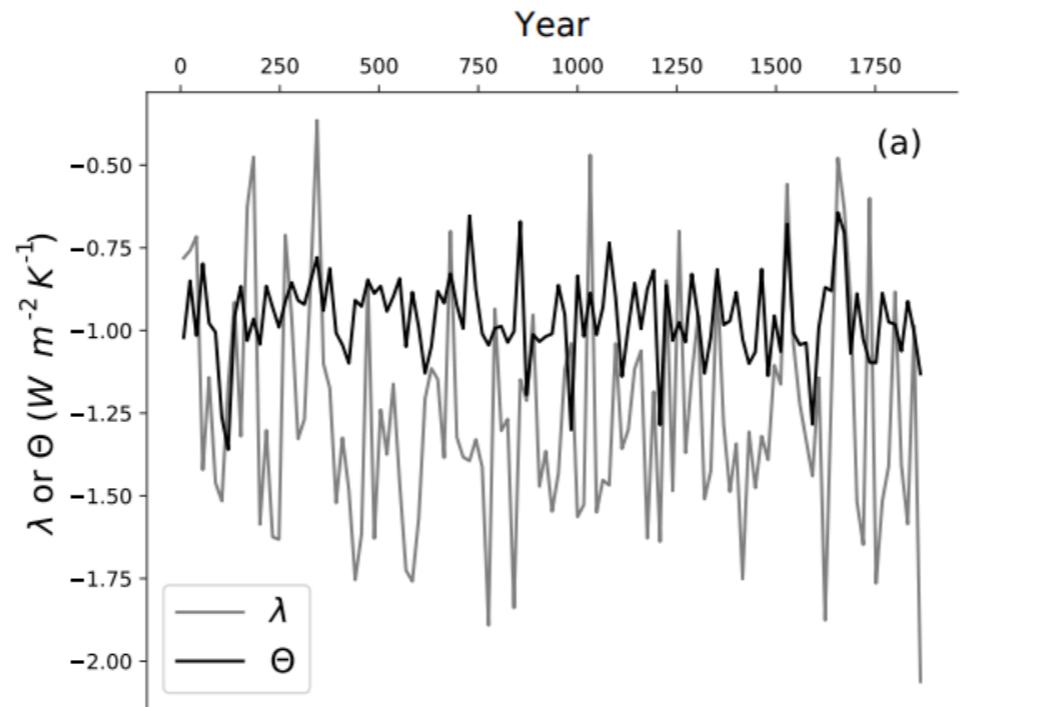
Names containing “all” or “good” include all models or just the ones whose  $\lambda_{iv}$  agrees with the CERES observations, respectively. The names with “-1” or “-2” use  $\lambda_{iv,obs}$  derived using estimates of forcing (the R-F calculations) and the detrended calculations, respectively. The names including “-f” use forcing from the CMIP5 abrupt 4x CO<sub>2</sub> runs (see Sect. S2). The names including “-f\_20-150” calculate F<sub>2xCO<sub>2</sub></sub> and  $\lambda_{4xCO_2}$  from years 20-150 of the abrupt 4xCO<sub>2</sub> runs (see Sect. S2).

Table 2. ECS values from the  $\Theta$  runs

Same as Table 1, but derived using Eq. 6.

<b>run</b>	<b>mean</b>	<b>mode</b>	<b>median</b>	<b>5-95%</b>	<b>17-83%</b>	<b>%&lt;2</b>	<b>%&gt;4.5</b>
all-Theta-1	3.33	2.58	3.14	0.7-6.2	2.1-4.6	15	19
all-Theta-2	2.96	2.31	2.82	0.7-5.4	1.9-4.1	20	11
all-Theta-1-corr	3.36	2.58	3.13	0.8-6.5	2.0-4.8	16	20
all-Theta-1-f	3.11	2.44	2.91	0.7-6.0	1.9-4.4	21	16
all-Theta-1-f 20_150	2.98	2.31	2.75	0.6-5.8	1.8-4.3	24	14
good-Theta-1	3.56	2.58	3.33	2.0-5.9	2.4-4.7	6	20
good-Theta-2	3.43	3.12	3.33	1.9-5.3	2.4-4.4	6	15
good-Theta-1-corr	3.58	2.44	3.33	1.9-6.2	2.3-4.8	7	21
good-Theta-1-f	2.81	2.17	2.65	0.5-5.1	1.8-3.9	25	10
good-Theta-1-f 20-150	2.71	2.03	2.51	0.4-5.0	1.7-3.8	30	9
noGISS-Theta-1	3.56	2.58	3.28	1.9-6.3	2.3-4.8	8	21
noGISS-Theta-2	3.18	2.31	2.94	1.7-5.5	2.1-4.2	13	12

Names follow the same convention as Table 1. The names including “noGISS-” include all models except the two GISS models. In the “-corr” calculations, each Monte Carlo value of ECS uses values of  $\Delta T_s/\Delta T_A$  and  $\Theta_{iv}/\Theta_{4xCO_2}$  from the same model.



**Figure 6.** **(a)** Time series of  $\lambda$  (gray) and  $\Theta$  (black) estimated in a 17-year sliding window of a 2000-year control run of the MPI-ESM1.1. **(b)** PDFs of the time series in **(a)**. Median and 5–95 % confidence interval for each distribution are displayed on the plot.